

Sequence comparison and alignment

		motif 2											
			193	195	198		217	ATP	ATP	231	233	235	
YstASP	293		KGKAY.LAQ	S	PQFNKQQLIV	ADFERVYEIG	PVFRAENSNT	HRHMT	EFTGL	DMEMAF	EEHY	HEVL	355
ThtASP	190		PGLFYALP	QS	PQLFKQMLMV	AGLDRYFQIA	RCFRDEDLRA	.DRQP	DFTQL	DLEMSF	.VEV	EDVL	251
EcoASP	184		KGKFYALP	QS	HQLFKQLLMM	SGFDRYYQIV	KCFRDEDLRA	.DRQPE	FTQI	DVETSF	.MTA	PQVR	245
EcoASN	191	QGVDFDKDF	FGKESFLT	VS	GQLNGETYAC	.ALSKIYTFG	PTFRAENSNT	SRHLAE	FWML	EPEVAF	.L	NDIA	262
YstASN	198	.NTSPTASSY	FGKPTYLT	VS	TQLHLEILAL	.SLSRCWTLS	PCFRAEKSDT	PRHLSE	FWML	EVEMCF	VNSV	NELT	269
ThtLYS	205	.PFKTYHNAL	DHEFY.L	RIS	LELYLKRLLV	GGYEKVFEIG	RNFRNEGIDH	.NHNPE	FTML	EAYWAY	.Y	QDMA	274
EcoLYS	221	.PFITHHNAL	DLDMY.L	RIA	PELYLKRLVV	GGFERVFEIN	RNFRNEGISV	.RHNPE	FTMM	ELYMAY	.Y	KDLI	290
YstLYS	284	.PFITHHNDL	DMDMY.M	RIA	PELFLKQLVV	GGLDRVYEIG	RQFRNEGIDM	.THNPE	FTTC	EFYQAY	.V	YDLM	353

Mastères Ingénierie et Chimie des BioMolécules et Biologie et Santé

Module Bioinformatique structurale. Cours I

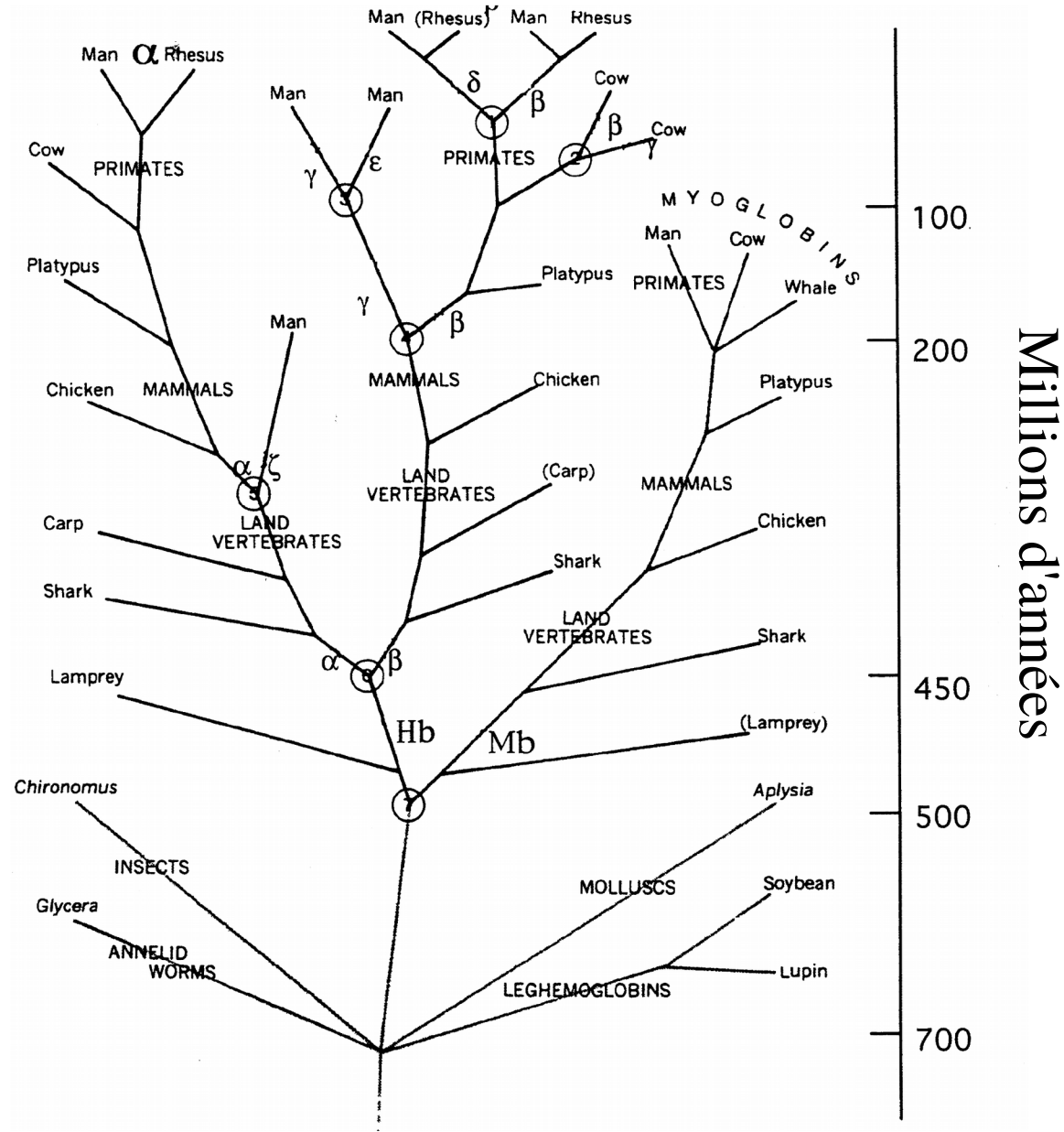
Novembre 2022

T. Simonson, Ecole Polytechnique



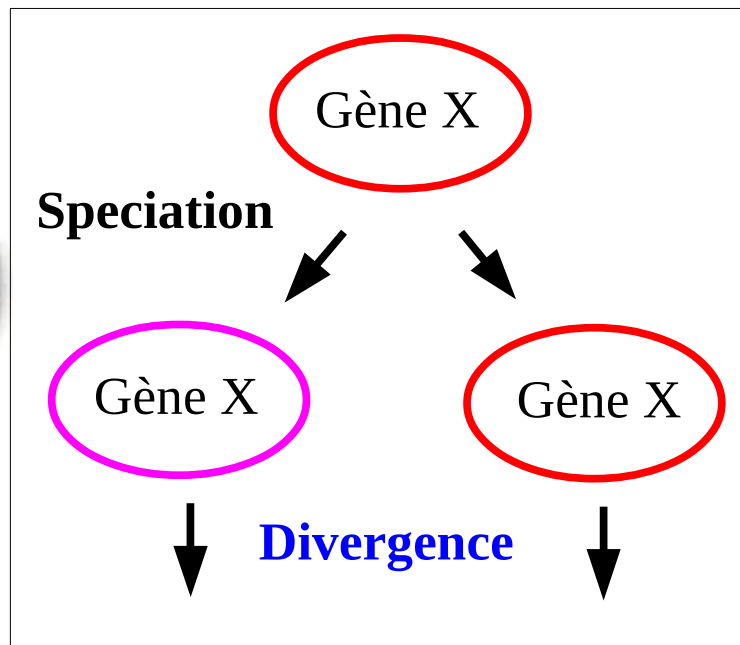
- **Sequence comparisons: what for?**
- **Sequence alignment as a model of evolution**
- **Sequence alignment: algorithms**

1) Similar proteins usually share a common ancestor: the globin example

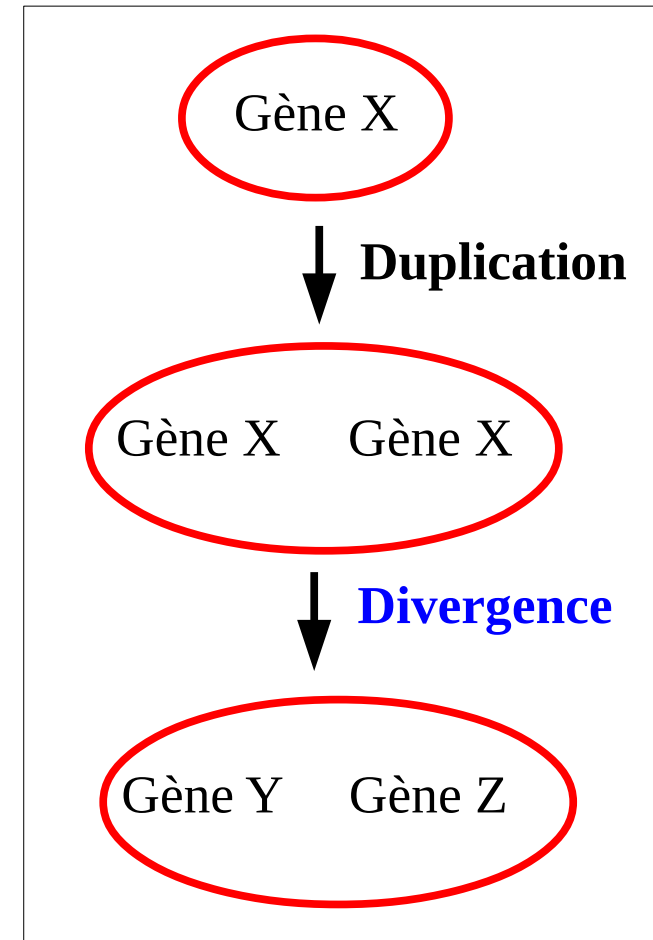


Phylogenetic tree
for globin evolution

Similar proteins usually share a common ancestor

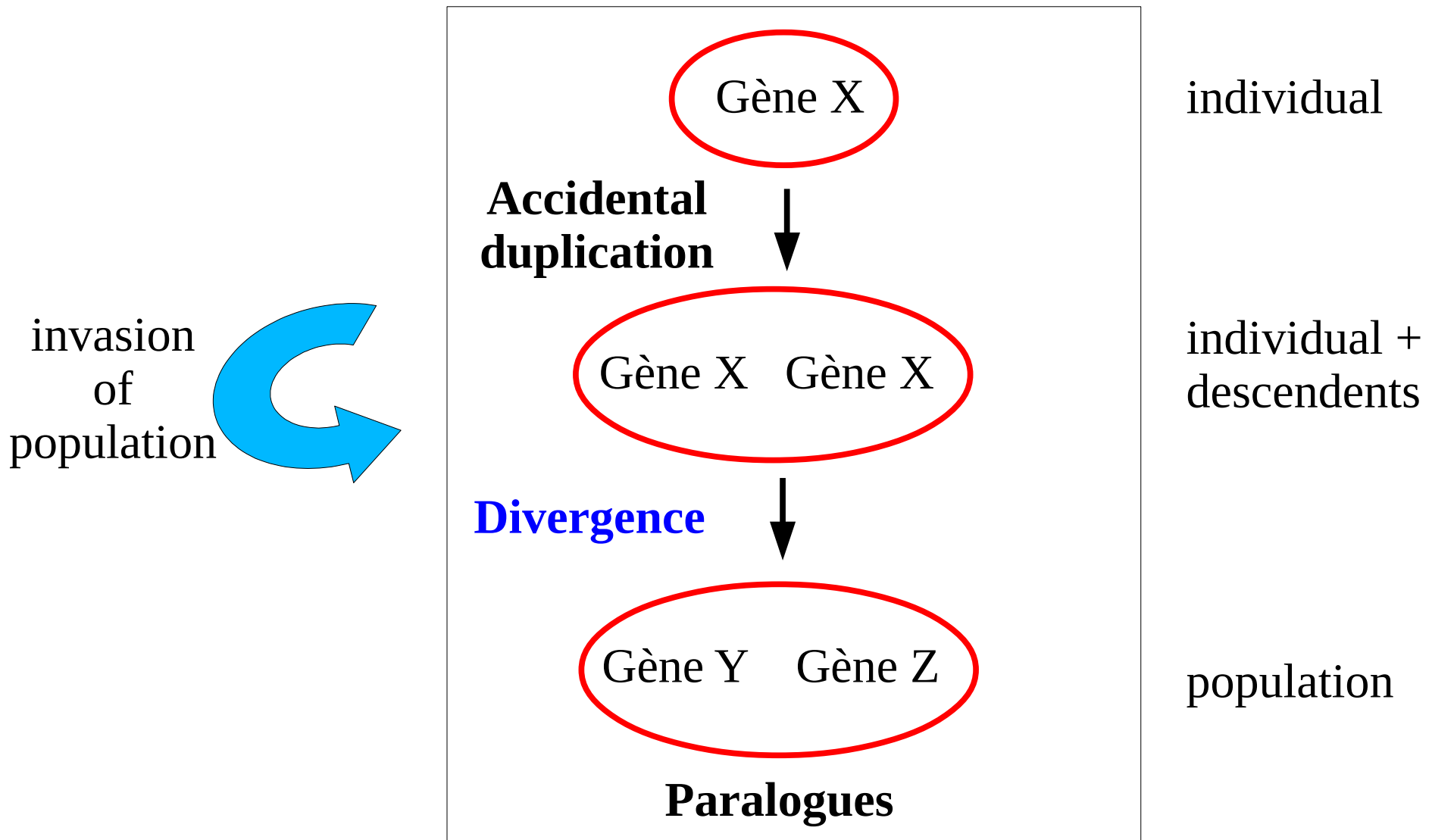


Orthologues



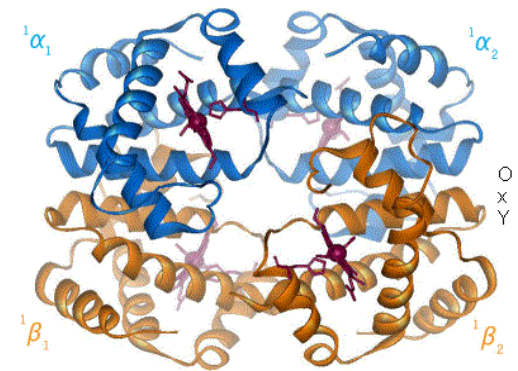
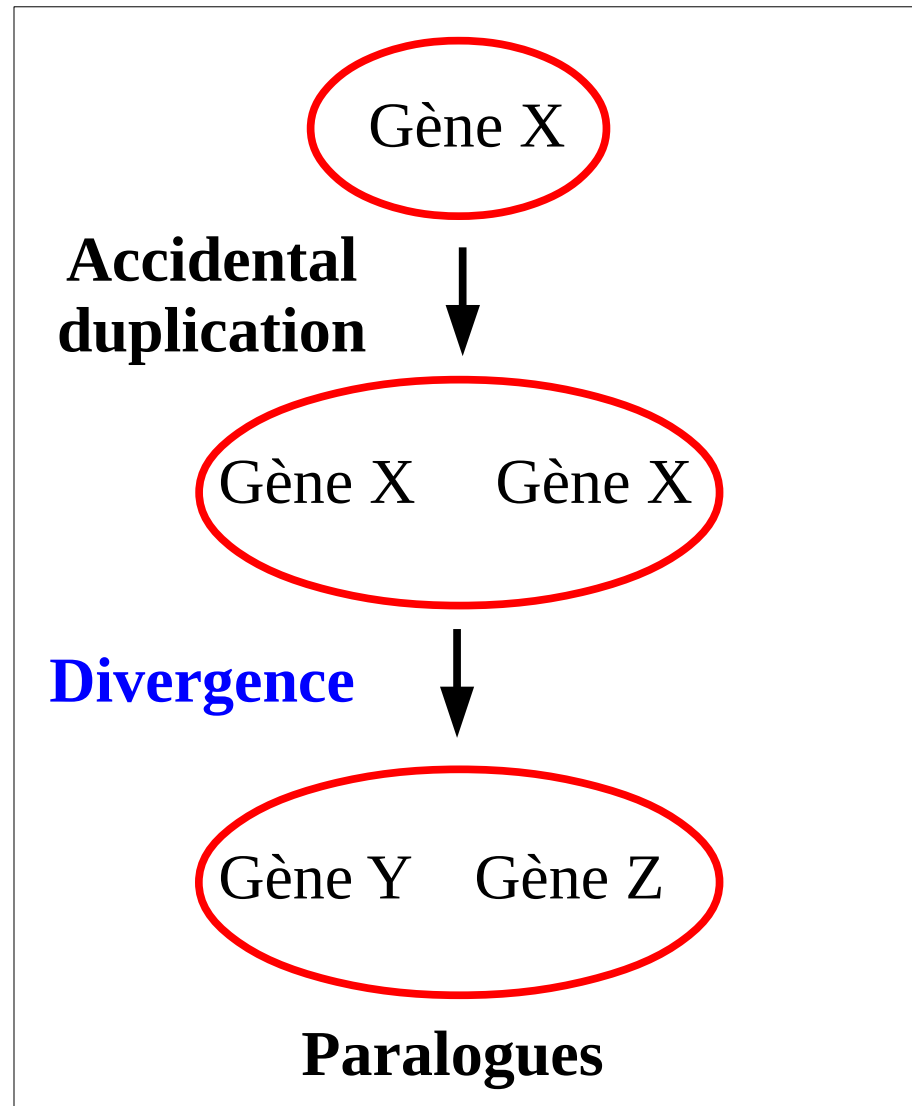
Paralogues

Duplication leads to paralogues



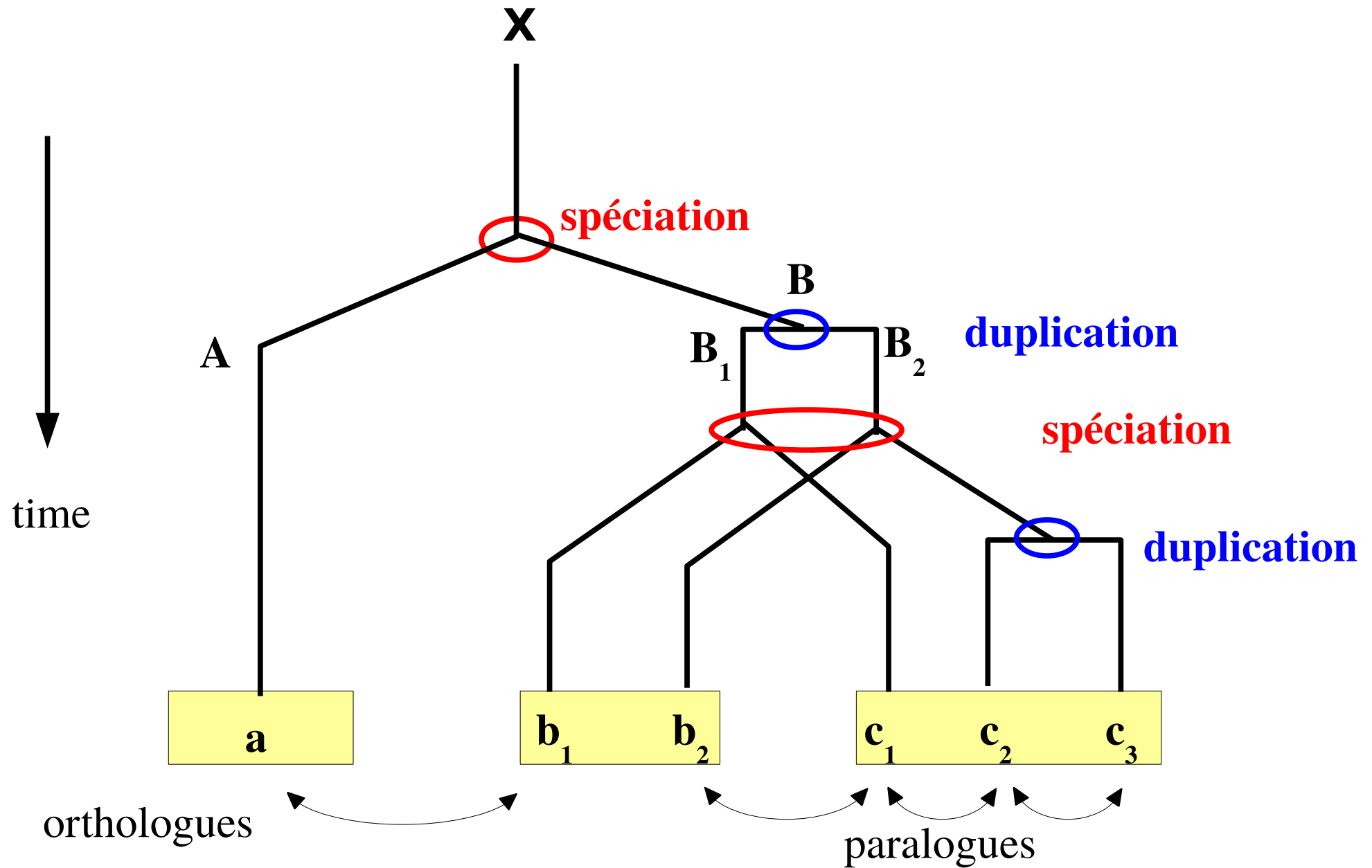
Paralogues usually change their function

Duplication leads to paralogues



Paralogues usually change their function

Evolution of a gene by speciation, duplication and divergence



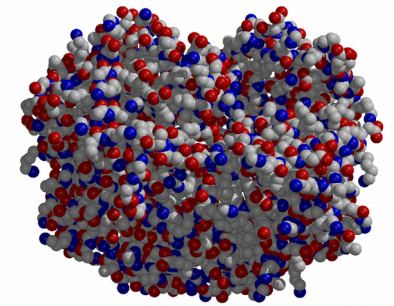
2) Similar proteins usually have similar structures and often have similar functions

K
L
H
G
G
P
M
L
D
S
D
Q
K
F
W
R
T
P
A
A
L

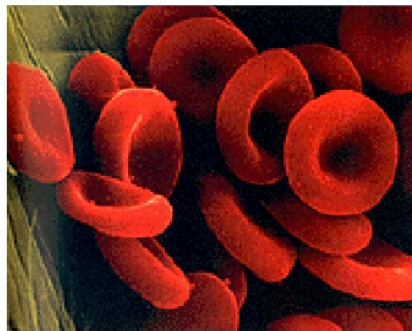
Sequence



Structure

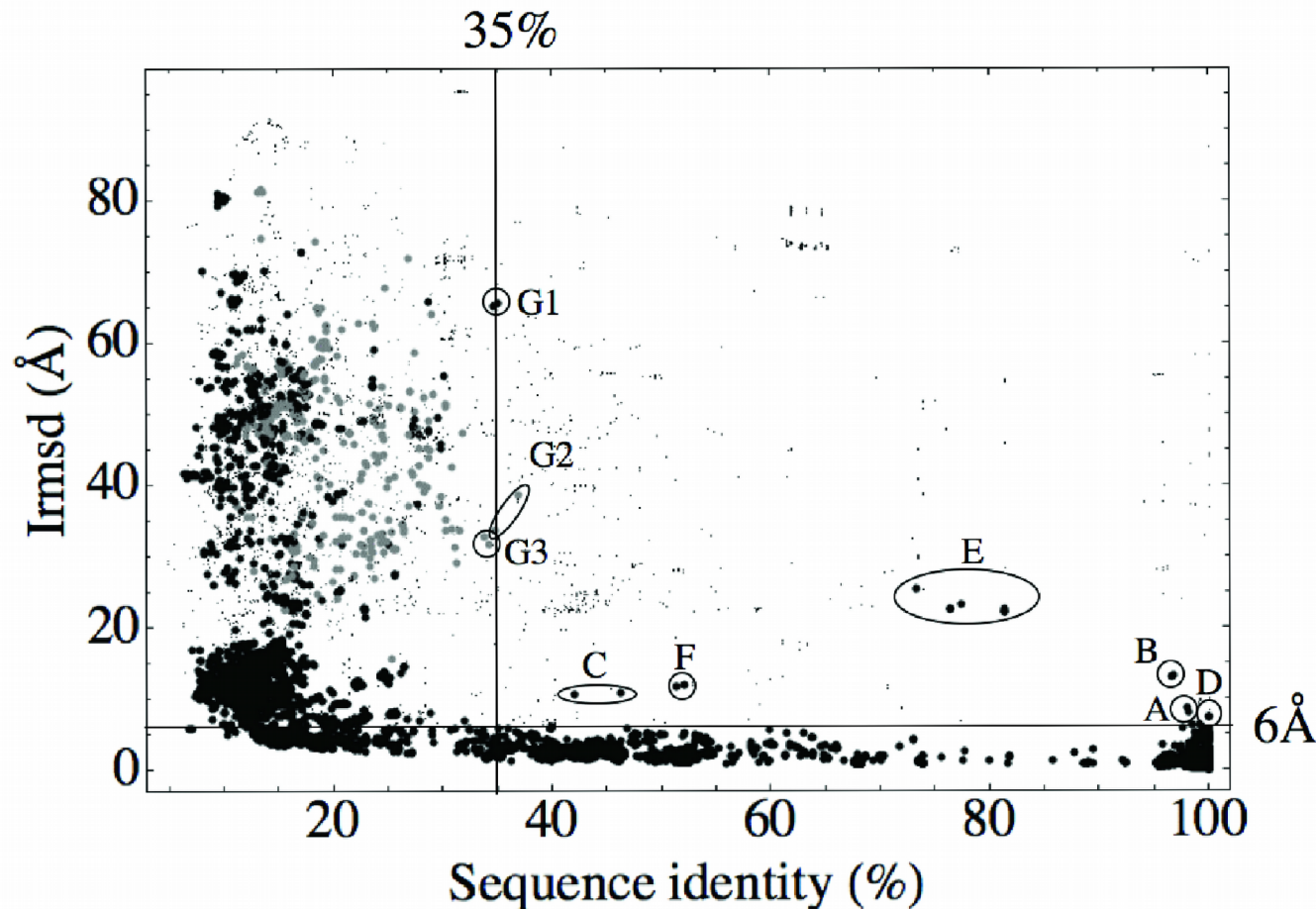


Function



Above 60% sequence identity, two homologs normally have the same function.

Above 35% sequence identity, homologous complexes usually interact in the same manner.



Launay & Simonson
BMC Bioinformatics
2008

Figure 1

The relationship between sequence and structural similarity. 743 complexes from 40 interacting superfamily groups (ISGs) were analyzed. All pairs within each ISG were compared, for a total of 9630 pairwise comparisons. Small points correspond to comparisons involving at least one complex with either a small interface (buried area < 600 Å²) or a weak association energy ($E_{int} > -10$ kcal/mol; see text). Points labelled A-G are discussed in the text. The horizontal line corresponds to Irmsd = 6 Å; the vertical line corresponds to a 35% sequence identity. Gray points correspond to comparisons where the MATRAS structural alignment provided fewer than 80% of the equivalent residues used for the Irmsd calculation. All the gray points lie below the 35% similarity threshold.

Sequence alignment as an evolutionary model

[illegible]

Alignment as a model of evolution

**Hypothesis: two similar proteins always
share a common ancestor**

Alignment as a hypothesis of a “parsimonious” common ancestor

T	C	L	I	C	G	D	E	A	S	G	C	H	Y	Androsterone receptor
T	C	L	V	C	G	D	E	A	T	G	Y	H	Y	Hypothetical common ancestor
L	C	V	V	C	G	D	K	A	T	G	Y	H	Y	Thyroid hormone receptor

Hypothetical mutations in red

Is the hypothesis likely?

A probabilistic model of evolution

$P(x_i, y_j)$ = probability to observe x_i aligned with y_j

$P(x_i \neq y_j)$ = $P(\text{"}x_i \text{ mutated to } y_j\text{" or "}y_j \text{ mutated to } x_i\text{"})$

$P(x_i = y_j)$ = $P(\text{"}x_i \text{ conserved"})$

sequence x:	T	C	L	I	C	G	D	E	A	S	G	C	H	Y
sequence y:	L	C	V	V	C	G	D	K	A	T	G	Y	H	Y

- Probabilities estimated from test alignements
- Assume positions are equivalent and independent

The likelihood or probability of an alignment

T C L I C G D E A S G C H Y Récepteur de l'androstérone

L C V V - G D K A T G Y H Y Récepteur de l'hormone thyroïdienne

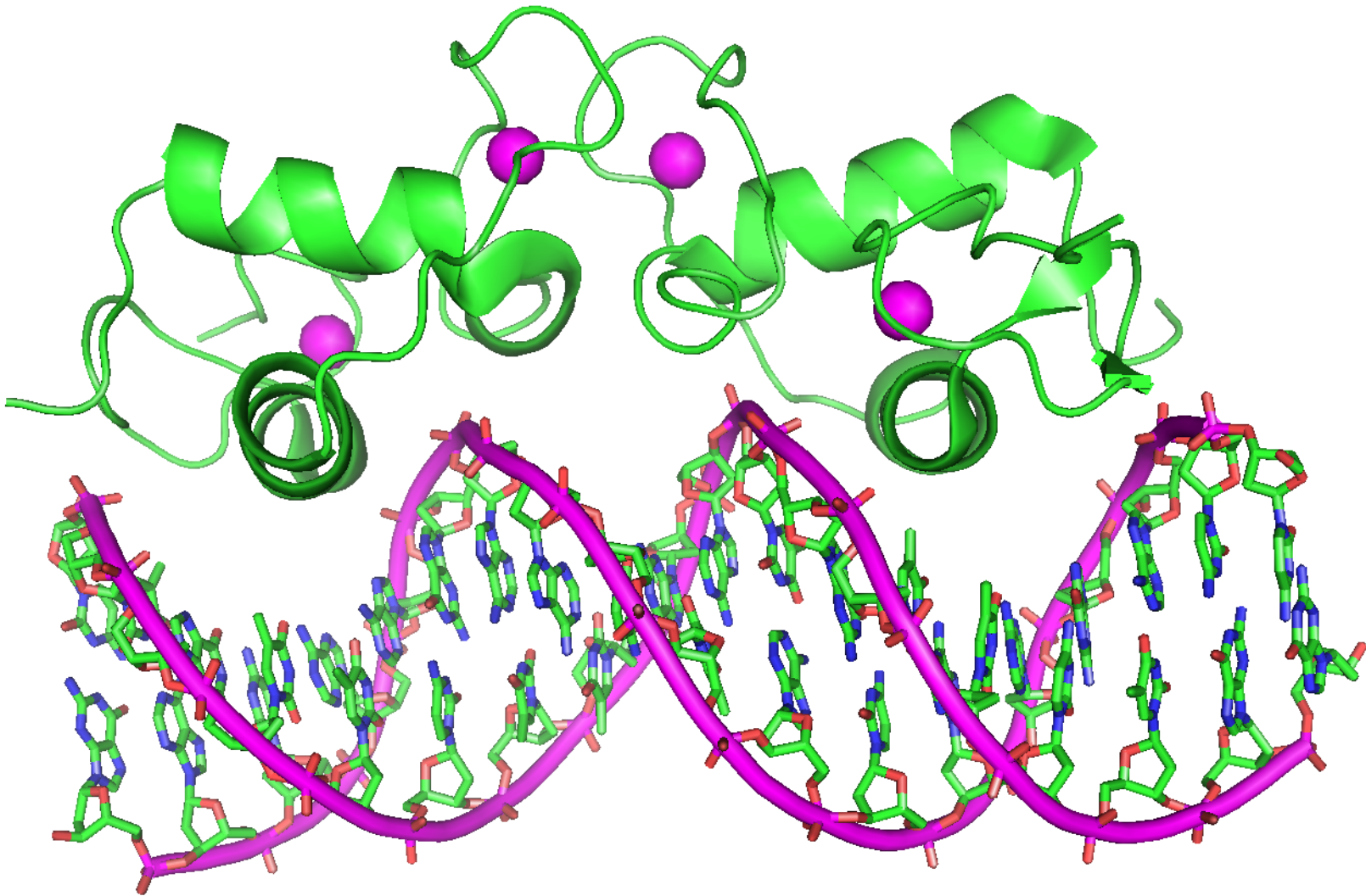
Probable mutations ➡ probable alignment

Improbable mutations ➡ improbable alignment

Comparing *homologous* proteins, we see that mutations have different probabilities

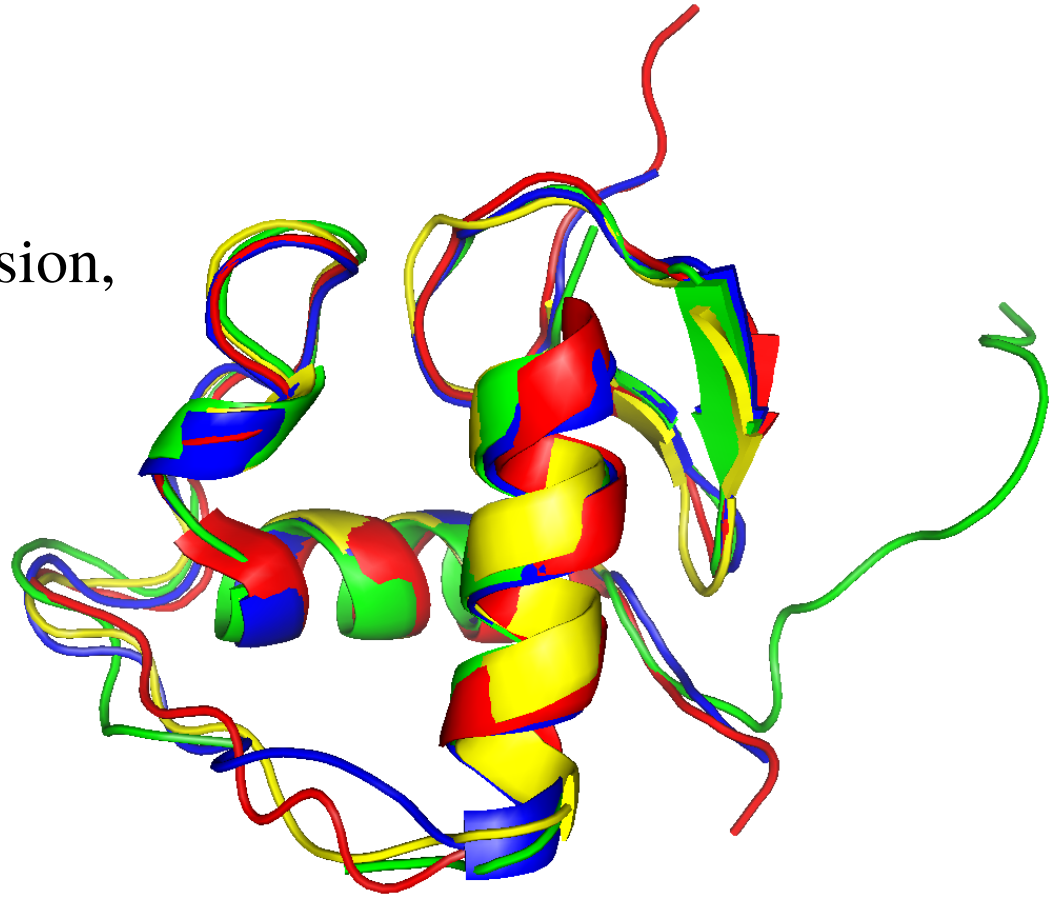
androgène	V	F	F	K	R	A	A	E	G	-	-	K	Q	K	Y	L	C	A	S	R	N	D	C	T	I	D	K	F	R	R	K	N	C	P	S	C	R	L	R	K	C	Y
progestérone	V	F	F	K	R	A	V	E	G	-	-	H	H	N	Y	L	C	A	G	R	N	D	C	I	V	D	K	I	R	R	K	N	C	P	A	C	R	L	R	K	C	Y
minéralocorticoïde	V	F	F	K	R	A	V	E	G	-	-	Q	H	N	Y	L	C	A	G	R	N	D	C	I	I	D	K	I	R	R	K	N	C	P	A	C	R	L	Q	K	C	L
glucocorticoïde	V	F	F	K	R	A	V	E	G	-	-	Q	H	N	Y	L	C	A	G	R	N	D	C	I	I	D	K	I	R	R	K	N	C	P	A	C	R	Y	R	K	C	L
estrogène	A	F	F	K	R	S	I	Q	G	-	-	H	N	D	Y	M	C	P	A	T	N	Q	C	T	I	D	K	N	R	R	K	S	C	Q	A	C	R	L	R	K	C	Y
acide rétonique	G	F	F	R	R	S	I	Q	K	-	-	N	M	V	Y	T	C	H	R	D	K	N	C	I	I	N	K	V	T	R	N	R	C	Q	Y	C	R	L	Q	K	C	F
vitamine D3	G	F	F	R	R	S	M	K	R	-	-	K	A	L	F	T	C	P	F	N	G	D	C	R	I	T	K	D	N	R	R	H	C	Q	A	C	R	L	K	R	C	V
thyroïde	G	F	F	R	R	T	I	Q	K	N	L	H	P	T	Y	S	C	K	Y	D	S	C	C	V	I	D	K	I	T	R	N	Q	C	Q	L	C	R	F	K	K	C	L
	*	*	:	*	:	.	:	:									*	:	*	*	.	*	**	:	:	*																

Récepteur de l'androstérone



Nuclear receptors

Bind DNA and regulate gene expression,
under the control of small
ligands: steroids, vitamins, ...



androgen
Rev Erb
glucocorticoid
retinoic acid

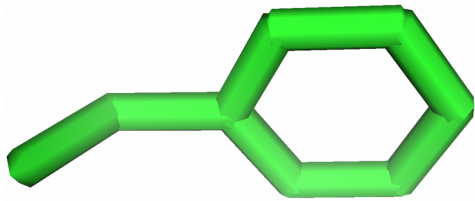
CLICGDEASGAHYGALTTCGSCKVFFKRAAEGKQKYL-CASRNDCTIDKFRRKNCPSCRLRKCYEAGMTLGA
CKVCGDVASGFHYGVLACEGCKGFFRRSIQQNIQYKRCLKNENCSIVRINRNRCCQCRFKKCLSVGMSRD-
CLVCSDEASGCHYGVLTCGCKAFFKRAVEGQHNYL-CKYEGKCIIDKIRRNKCPACRYRKCLQAGMNLEA
CAICGDRSSGKHYGVYSCEGCKGFFKRTVRKDLTYT-CRDNKDCLIDKRQRNRCQYCRYQKCLAMGM- - -

Mutations have different probabilities

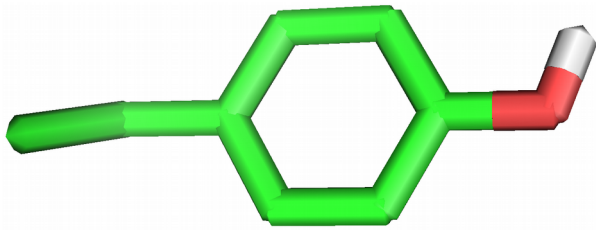
androgène	VFFKRAAEG--KQKYL	CASRNDCTIDKFRRKNCPSCRLRKCY
progestérone	VFFKRAVEG--HHNYLC	AGRNDCIIVDKIRRRKNCPACRLRKCY
minéralocorticoïde	VFFKRAVEG--QHNYLC	AGRNDCIIDKIRRRKNCPACRLQKCL
glucocorticoïde	VFFKRAVEG--QHNYLC	AGRNDCIIDKIRRRKNCPACRYRKCL
estrogène	AFFKRSIQG--HNDYMC	PATNQCTIDKNRRKSCQACRLRKCY
acide rétinolique	GFFRRSIQK--NMVYT	CHRDKNCIINKVTRNRCQYCRLQKCF
vitamine D3	GFFRRSMKR--KALFT	CPFNGDCRITKDNRRHRCQACRLKRCV
thyroïde	GFFRRTIQKNLHPTYS	CKYDSCCVIDKITRNQCQLCRFKKCL
	**:*:*:	*:*:*:*:*



Different amino acid structures yield different probabilities



PHE
F



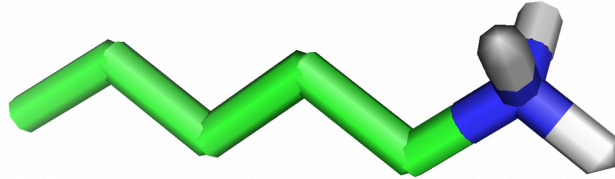
TYR
Y

homologues

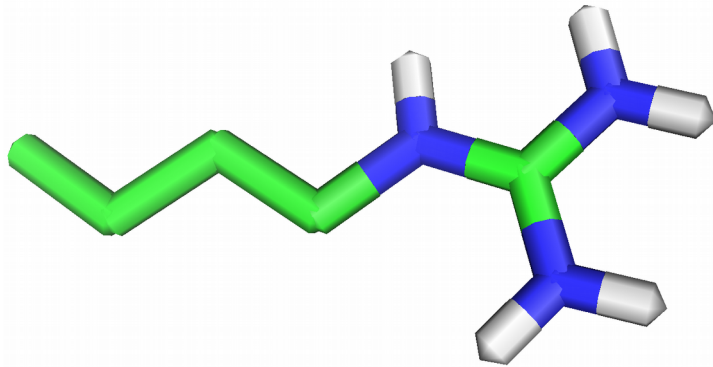
KYL
NYL
NYL
NYL
DYM
VYT
LFT
TYS
:

Different amino acid structures yield different probabilities

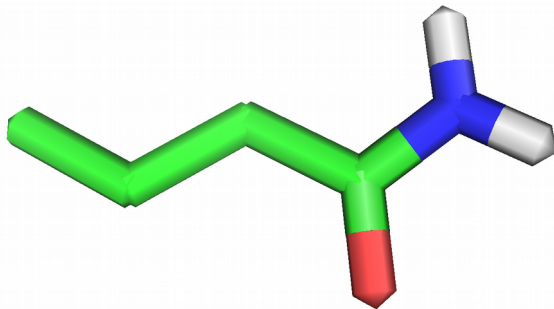
LYS
K



ARG
R



GLN
Q



homologues

RKCY
RKCY
QKCL
RKCL
RKCY
QKCF
KRCV
KKCL
⋮ *

A probabilistic model of evolution

$P(x_i, y_j)$ = probability to observe x_i aligned with y_j

$P(x_i \neq y_j)$ = $P(\text{“}x_i \text{ mutated to } y_j\text{” or “}y_j \text{ mutated to } x_i\text{”})$

$P(x_i = y_j)$ = $P(\text{“}x_i \text{ conserved”})$

sequence x:	T	C	L	I	C	G	D	E	A	S	G	C	H	Y
sequence y:	L	C	V	V	C	G	D	K	A	T	G	Y	H	Y

- Probabilities estimated from test alignements
- Assume positions are equivalent and independent

Problem: what is a large probability?

Alignement avec le récepteur humain de la progestérone

```
PQKTCLICGDEASGAHYGALTCGSCKVFFKRAAEGKQKYL CASRNDCTIDKFRRKNCPSC
PQRVVICGDEASGCHYGVLTTCGSCKVFFKRAVEGHHQYLCAGRNDICVDKIRRKNCPAC
* * | * | * * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
```

Alignement avec le récepteur humain de l'hormone thyroïdienne

```
PQKTCLICGDEASGAHYGALTCGSCKVFFKRAAEG - -KQKYL CASRNDCTIDKFRRKNCPSC
KDEQCVVCGDKATGYHYRCITCEGCKGFFRRTIQKNLHPTYSCKYDSCCVIDKITRNQCQLC
* | | * * * | * | * * * | * * * * * * * * * * * * * * * * * * * * *
```

Alignement avec la ferrédoxine de la bactérie *Proteus vulgaris*

```
PQKTCLICGDEASGAHYGTLTCGSCKVFFKRAAEGKQKYL CASRNDCTIDKFRRKNCPSC
DQDKCIGCKTCVLACPYGTMEVVS RPVMRKL TALNTIEAFKAEANKCDLCHHRAEG - PAC
* * | * * * * * * * * * * * * * * * * * * * * * * * * * * * * *
```

“Random” model as a reference

Evolutionary hypothesis: two sequences have a (parsimonious) common ancestor

Null hypothesis: they have no biological relation: compute probability as if the sequences were random

$Q(x_i, y_j)$ = probability to observe x_i and y_j
in two independent proteins

= $q_{xi} q_{yj}$ Natural frequencies of x_i, y_j

x	q_x	
W	1.3 %	of amino acids
L	9.0 %	

W L
≠
W L

Likelihood of an alignment column

We compute the ratio between the probabilities P (evolutionary case) and Q (random case):

def.

$$M(x_i, y_j) = \log P(x_i, y_j) / Q(x_i, y_j)$$

$$= \log [P(x_i, y_j) / q_{x_i} q_{y_j}]$$

x_i														
	T	C	L	I	C	G	D	E	A	S	G	C	H	Y
	L	C	V	V	C	G	D	K	A	T	G	Y	H	Y
y_i														

M = scoring matrix

Matrix example: BLOSUM62

	C	S	T	P	A	G	N	D	E	Q	H	R	K	M	I	L	V	F	Y	W	
C	9	-1	-1	-3	0	-3	-3	-3	-4	-3	-3	-3	-3	-1	-1	-1	-1	-2	-2	-2	C
S		4	1	-1	1	0	1	0	0	0	-1	-1	0	-1	-2	-2	-2	-2	-2	-3	S
T			5	-1	0	-2	0	-1	-1	-1	-2	-1	-1	-1	-1	-1	0	-2	-2	-2	T
P				7	-1	-2	-2	-1	-1	-1	-2	-2	-1	-2	-3	-3	-2	-4	-3	-4	P
A					4	0	-2	-2	-1	-1	-2	-1	-1	-1	-1	-1	0	-2	-2	-3	A
G						6	0	-1	-2	-2	-2	-2	-2	-3	-4	-4	-3	-3	-3	-2	G
N							6	1	0	0	1	0	0	-2	-3	-3	-3	-3	-2	-4	N
D								6	2	0	-1	-2	-1	-3	-3	-4	-3	-3	-3	-4	D
E									5	2	0	0	1	-2	-3	-3	-2	-3	-2	-3	E
Q										5	0	1	1	0	-3	-2	-2	-3	-1	-2	Q
H											8	0	-1	-2	-3	-3	-3	-1	2	-2	H
R												5	2	-1	-3	-2	-3	-3	-2	-3	R
K													5	-1	-3	-2	-2	-3	-2	-3	K
M														5	1	2	1	0	-1	-1	M
I															4	2	3	0	-1	-3	I
L																4	1	0	-1	-2	L
V																	4	-1	-1	-3	V
F																		6	3	1	F
Y																			7	2	Y
W																				11	W
	C	S	T	P	A	G	N	D	E	Q	H	R	K	M	I	L	V	F	Y	W	

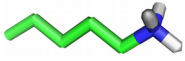
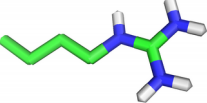
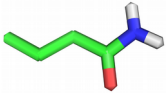
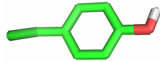
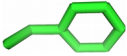
Matrix example: BLOSUM62

	C	S	T	P	A	G	N	D	E	Q	H	R	K	M	I	L	V	F	Y	W	
C	9	-1	-1	-3	0	-3	-3	-3	-4	-3	-3	-3	-3	-1	-1	-1	-1	-2	-2	-2	C
S		4	1	-1	1	0	1	0	0	0	-1	-1	0	-1	-2	-2	-2	-2	-2	-3	S
T			5	-1	0	-2	0	-1	-1	-1	-2	-1	-1	-1	-1	-1	0	-2	-2	-2	T
P				7	-1	-2	-2	-1	-1	-1	-2	-2	-1	-2	-3	-3	-2	-4	-3	-4	P
A					4	0	-2	-2	-1	-1	-2	-1	-1	-1	-1	-1	0	-2	-2	-3	A
G						6	0	-1	-2	-2	-2	-2	-2	-3	-4	-4	-3	-3	-3	-2	G
N							6	1	0	0	1	0	0	-2	-3	-3	-3	-3	-2	-4	N
D								6	2	0	-1	-2	-1	-3	-3	-4	-3	-3	-3	-4	D
E									5	2	0	0	1	-2	-3	-3	-2	-3	-2	-3	E
Q										5	0	1	1	0	-3	-2	-2	-3	-1	-2	Q
H											8	0	-1	-2	-3	-3	-3	-1	2	-2	H
R												5	2	-1	-3	-2	-3	-3	-2	-3	R
K													5	-1	-3	-2	-2	-3	-2	-3	K
M														5	1	2	1	0	-1	-1	M
I															4	2	3	0	-1	-3	I
L																4	1	0	-1	-2	L
V																	4	-1	-1	-3	V
F																		6	3	1	F
Y																			7	2	Y
W																				11	W
	C	S	T	P	A	G	N	D	E	Q	H	R	K	M	I	L	V	F	Y	W	

Penalty for gaps: see below

Exc: compute $P(W,W)$ and $P(L,L)$ and comment.

Mutations have different probabilities

		K	R	Q	Y	F
	K	6	3	2	-2	-4
	R		7	1	-1	-3
	Q			7	-1	-4
	Y				8	4
	F					8

BLOSUM50 matrix

Likelihood or probability of an alignment

$P(x_i, y_j)$ = probability to observe x_i aligned with y_j

= $P(\text{"}x_i \text{ conserved" or "}x_i \text{ mutated to } y_j \text{" or "}y_j \text{ mutated to } x_i \text{"})$

T	C	L	I	C	G	D	E	A	S	G	C	H	Y
L	C	V	V	-	G	D	K	A	T	G	Y	H	Y

- Probabilities from test alignments
- Assume equivalent positions
- Assume independent positions: $P(\text{alignment}) = \prod_{(i,j)} P(x_i, y_j)$

Likelihood or probability of an alignment

$$\begin{aligned} s(x_i, y_j) &= \log P(x_i, y_j) / Q(x_i, y_j) \\ &= \log [P(x_i, y_j) / q_{xi} q_{yj}] \end{aligned}$$

$$s(x, y) = \sum_{(i,j)} s(x_i, y_j)$$

T	C	L	I	C	G	D	E	A	S	G	C	H	Y
L	C	V	V	-	G	D	K	A	T	G	Y	H	Y

Mutation probability depends on time

$P(x,y) = P(x,y;T)$ = probability of a mutation during time T

Cytochromes c from chimpanzee and human
are closer than those from
human and Escherichia coli...

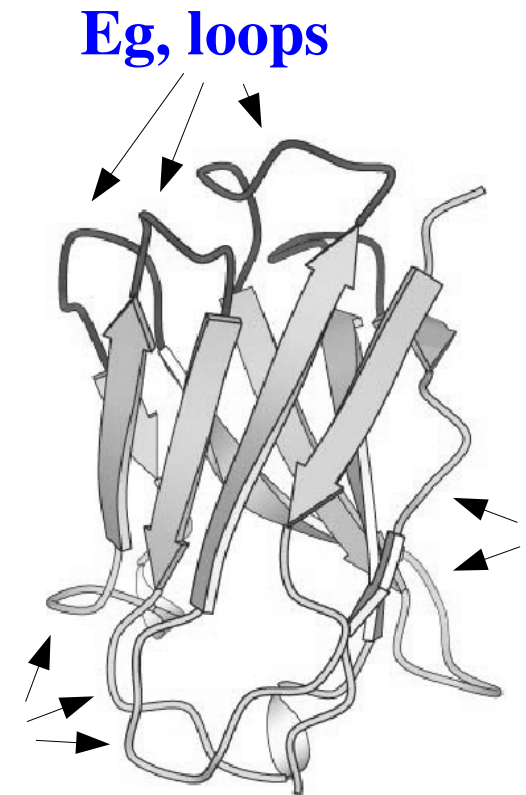
A similarity matrix is valid for a certain time scale,
or similarity scale

BLOSUM50 $\neq$ BLOSUM62

Better gap treatment

It is easier to *extend* a gap than open a new one

- Open a gap: $-d$
- Extend by one residue: $-e$ ($e < d$)
- Cost of a gap of length m :
$$g(m) = -d - (m-1) e$$



Positions are no longer equivalent nor independent

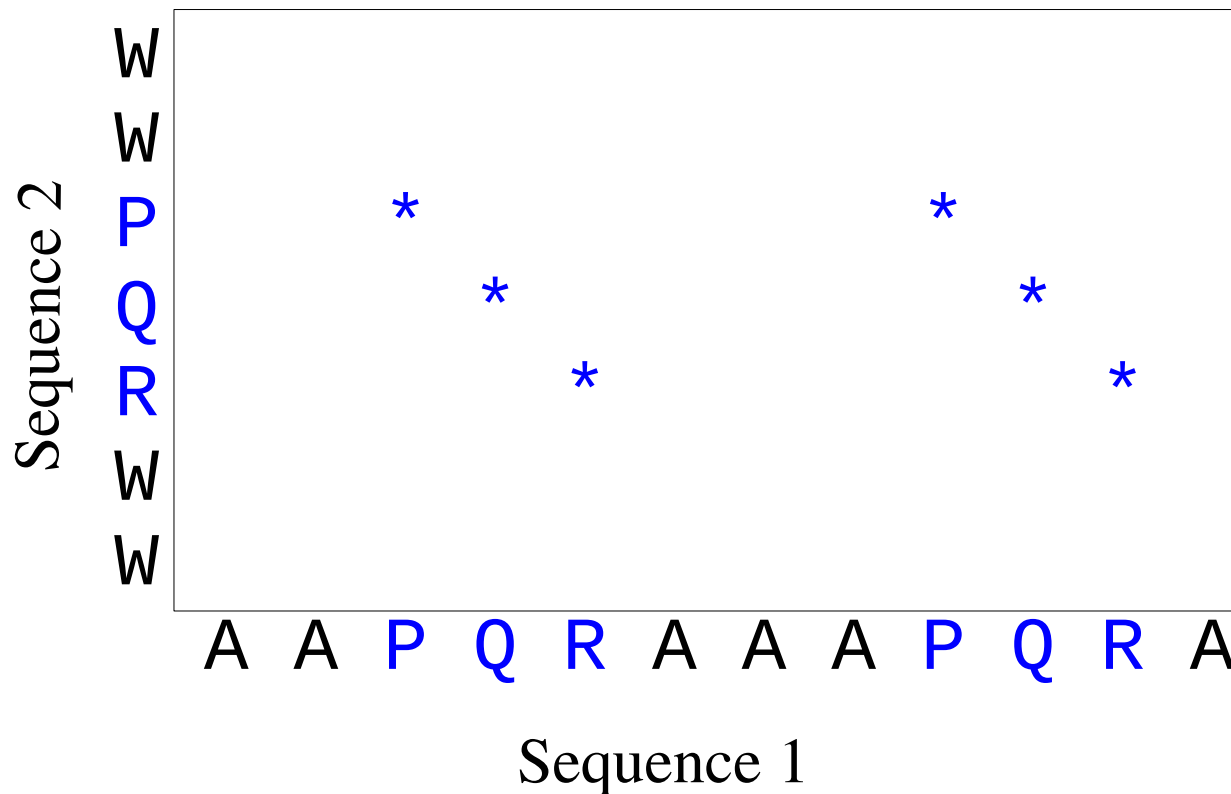
An alignment represents a model of evolution, with:

- Minimal divergence from a common ancestor
- Empirical mutation probabilities
- Assumption of equivalent and independent positions
- A simple Null hypothesis

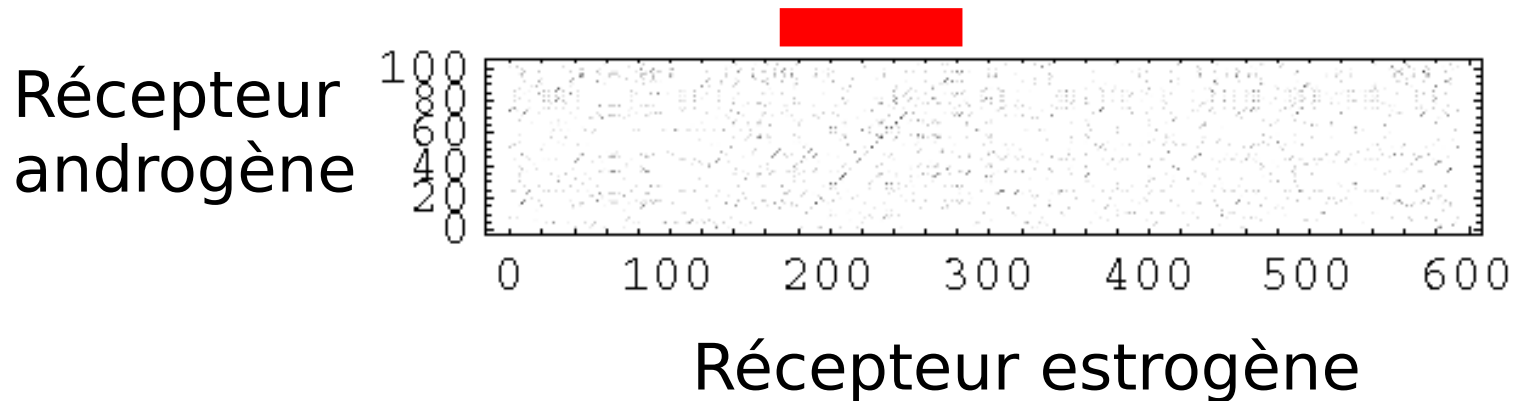
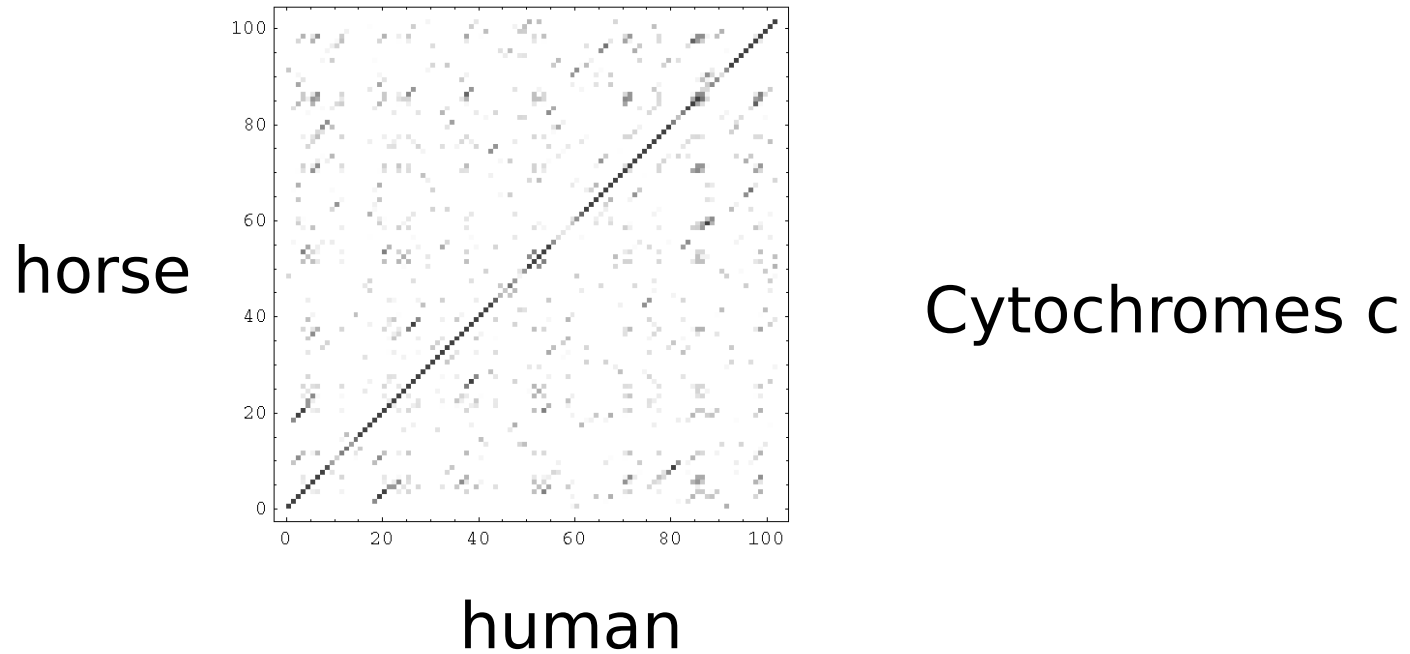
Sequence alignment algorithms

Graphical sequence comparison

Each sequence is written on the edge of a table or matrix. For similar residue pairs, one inserts a similarity symbol:



Graphical sequence comparison



Often only part of a protein is conserved: Need for a ‘local’ alignment



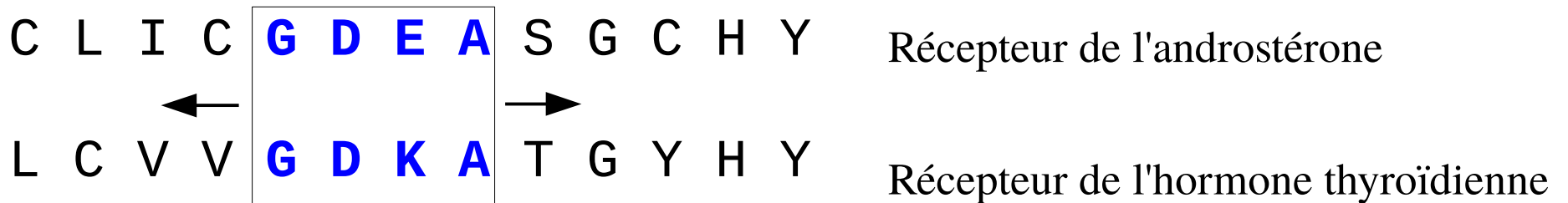
Aspartyl-tRNA
synthetase
from yeast



Active site domain,
Aspartyl-tRNA
synthetase
from E coli

BLAST: *Basic Local Alignment Search Tool*

- Find homologous tetrapeptides
- Extend each peptide as long as similarity > threshold



Tetrapeptides homologous to a query tetrapeptide

G	D	E	A	score
BLOSUM62				
G	D	E	A	21 = 6+6+5+4
G	D	D	A	18
G	D	Q	A	18
G	E	E	A	17
G	D	E	G	17
G	D	K	A	17
G	D	E	V	17

BLOSUM62

	V	A	G	D	E	Q	K
A	0	4					
G			6				
D				6	2		
E					5	2	1

7 homologues (using BLOSUM62 and a threshold of 17)

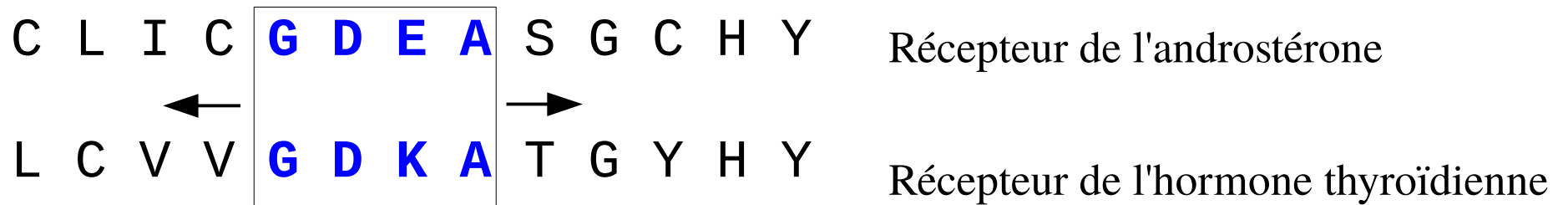
Find tetrapeptides that are homologous to query

G	D	E	A
G	D	D	A
G	D	Q	A
G	E	E	A
G	D	E	G
G	D	K	A
G	D	E	V

Tetrapeptides
homologous
to **GDEA**

>sp|P10827|THA_HUMAN **Thyroid hormone receptor** alpha Homo sapiens.
MEQKPSKVECGSDPEENSARSPDGKRKRKNGQCSLKTSMGYIPSYLDKDEQCVVC**GDKA**
TGYHYRCITCEGCKGFFRRTIQKNLHPTYSCKYDSCCVIDKITRNQCQLCRFKKCIAVGM
AMDLVLDDSKRVAKRKLIEQNRERRRKEEMIRSLQQRPEPTPEEWDLIHIATEAHRSTNA
QGSHWKQRRKFLPDDIGQSPIVSMPDGDKVDLEAFSEFTKIITPAITRVVDFAKKLPMFS
ELPCEDQIILLKGCCMEIMSLRAAVRYDPESDTLTLSGEMAVKREQLKNGGLGVVSDAIF
ELGKSLSAFNLDDTEVALLQAVLLMSTDRLGLLCVDKIEKSQEAYLLAFEHYVNHHRKHNI
PHFWPKLLMKEREVQSSILYKGAAAEGRPGGSLGVHPEGQQLLGMHVVQGPQVRQLEQQL
GEAGSLQGPVLQHQPSPKSPQQRLLLELLHRSGILHARAVCGEDDSSEADSPSSSEEEPEVC
EDLAGNAASP

**Extend “micro-alignment” in each direction,
as long as score > threshold**



- Each tetrapeptide leads to a local alignment without gaps
- Keep the best alignments

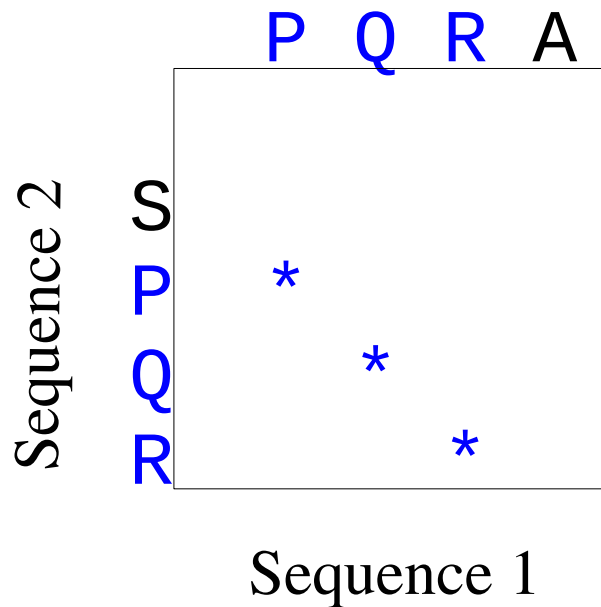
Homologues of the androsterone receptor identified using BLAST

#	ID Swissprot	Hit	Description	Score (bits)	% E Identity*	Match Length	
1	P15207	ANDR_RAT	Androgen receptor.	162	1e-40	100	73
6	P19091	ANDR_MOUSE	Androgen receptor.	162	1e-40	100	73
14	Q63449	PRGR_RAT	Progesterone receptor (PR)	136	1e-32	80	72
17	P06401	PRGR_HUMAN	Progesterone receptor (PR)	136	1e-32	80	72
21	P08235	MCR_HUMAN	Mineralocorticoid receptor (MR)	136	1e-32	79	72
33	P04150	GCR_HUMAN	Glucocorticoid receptor (GR)	131	3e-31	77	72
41	Q9YH32	ESR2_ORENI	Estrogen receptor beta (ER-beta)	99	3e-21	58	72
42	Q9YH33	ESR1_ORENI	Estrogen receptor (ER-alpha)	98	4e-21	55	72
:	:	:	:	:	:	:	:
:	:	:	:	:	:	:	:
343	Q9N4Q7	NH13_CAEEL	Nuclear hormone receptor nhr-13	54	8e-08	39	66
344	Q23294	NH11_CAEEL	Nuclear hormone receptor nhr-11	54	8e-08	42	66
345	O45460	NH54_CAEEL	Nuclear hormone receptor nhr-54	54	1e-07	37	67
346	Q09565	NH20_CAEEL	Nuclear hormone receptor nhr-20	51	7e-07	34	66
347	Q09587	NH22_CAEEL	Nuclear hormone receptor nhr-22	45	5e-05	32	66
349	P17672	E75B_DROME	Ecdysone-induced protein 75B	40	0.001	37	47
351	P20659	TRX_DROME	Trithorax protein.	31	0.74	26	49
355	P98164	LRP2_HUMAN	Lipoprotein receptor.	30	1.7	27	65

*E = expectation of number of random alignments with a higher score

A rigorous method, inspired by the previous “matrix”

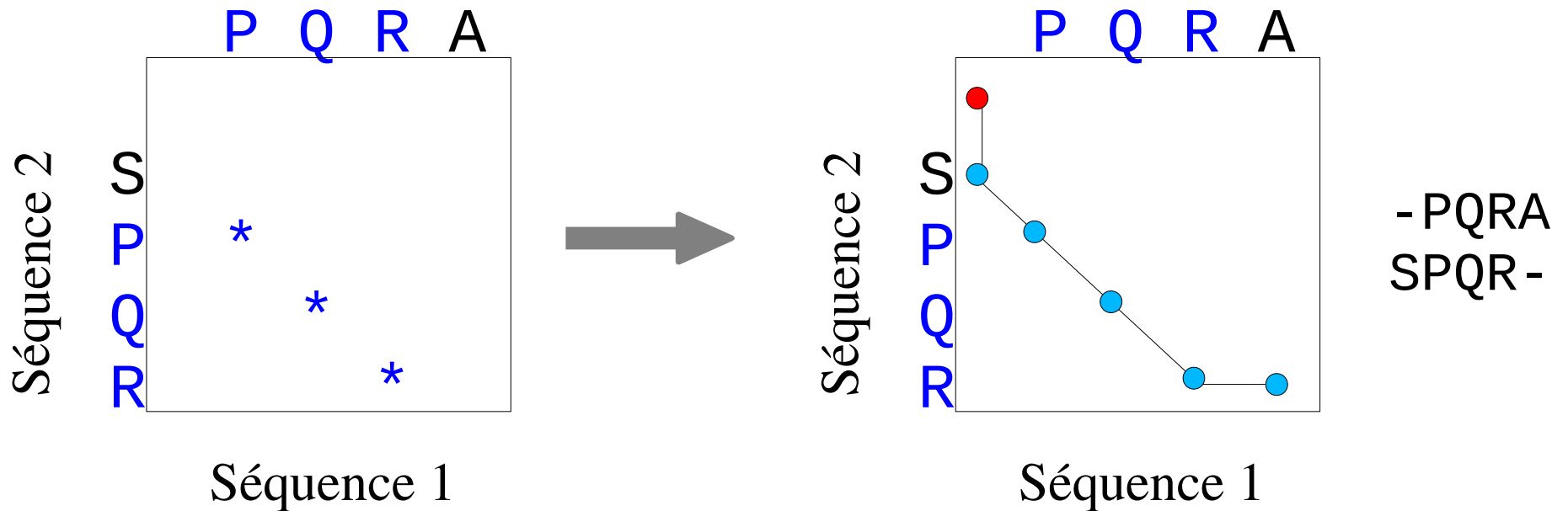
The sequences are written along the edges of the matrix:



A rigorous method; partial description

The sequences are written along the edges of the matrix.

An alignment is a path through the matrix:



Exc: represent the alignments:

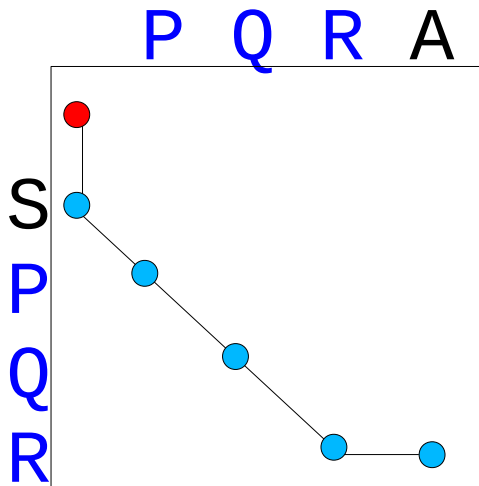
P - QRA
SPQR -

P - - QRA
SPQ - R -

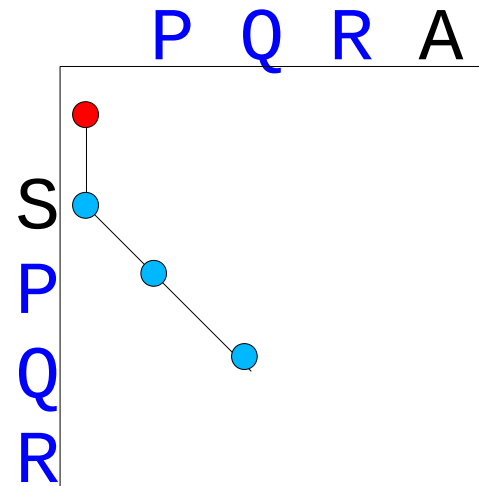
A rigorous method; partial description

The sequences are written along the edges of the matrix.

An incomplete path represents an incomplete alignment:



- PQRA
SPQR-

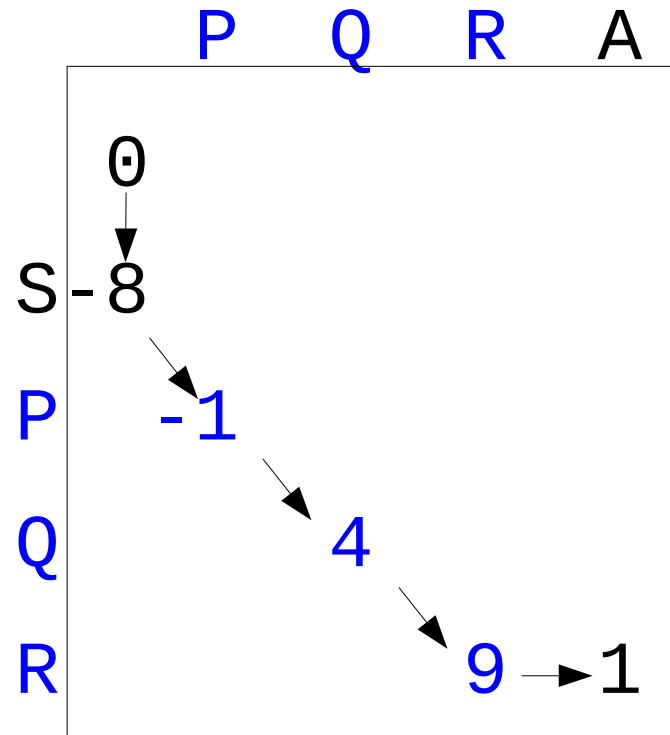
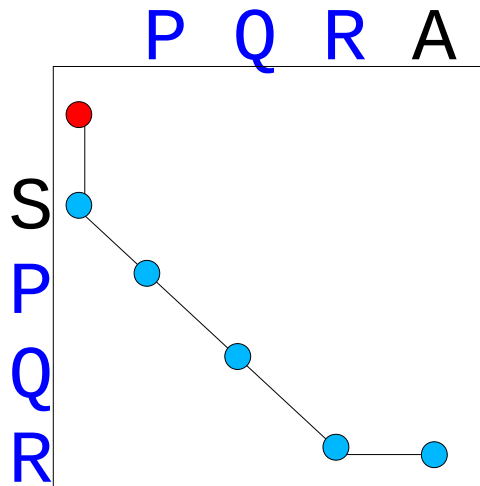


- PQ
SPQ

A rigorous method; partial description

The sequences are written along the edges of the matrix.

We annotate the matrix with the scores:

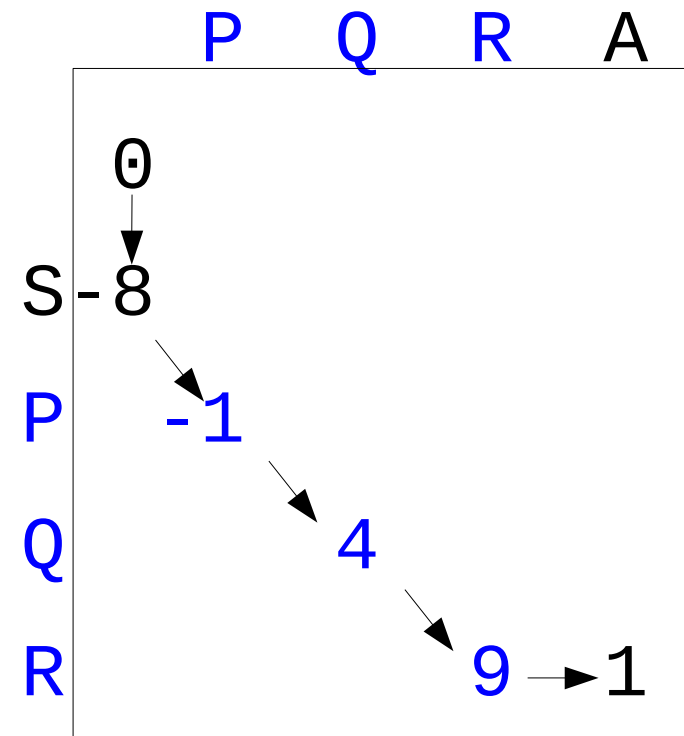


	S	P	Q	R
P	-1	7	-1	-2
Q	0	-1	5	1
R	-1	-2	1	5
A	1	-1	-1	-1

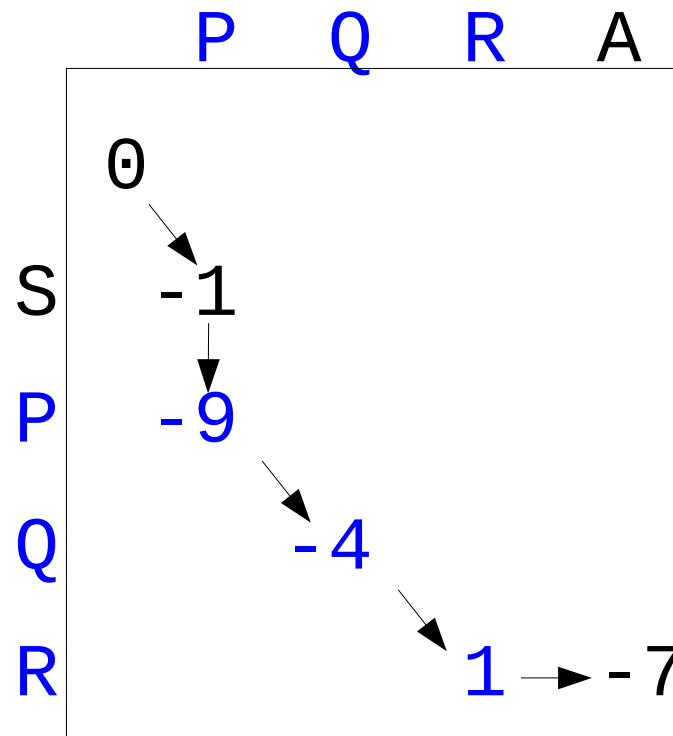
- PQRA
SPQR -

A rigorous method; partial description

The best alignment competes with many others:



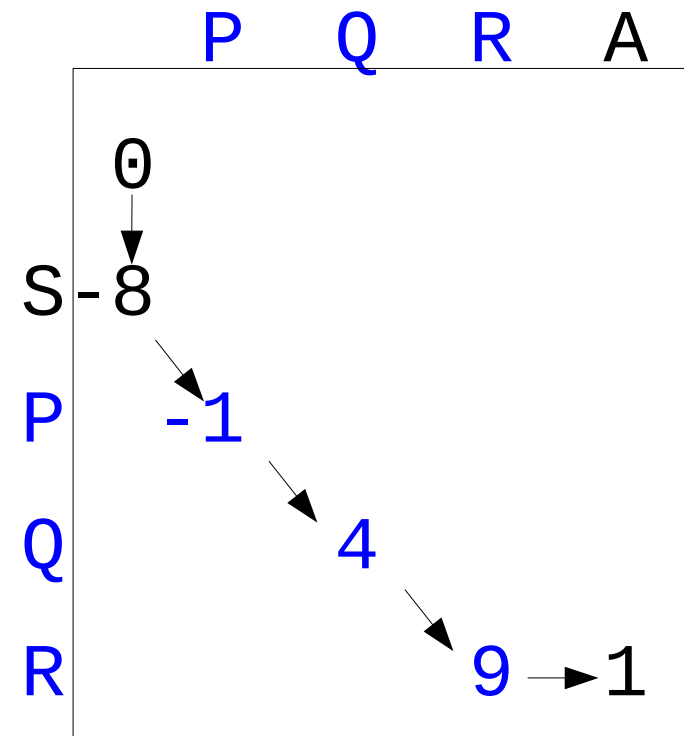
-PQRA
SPQR-



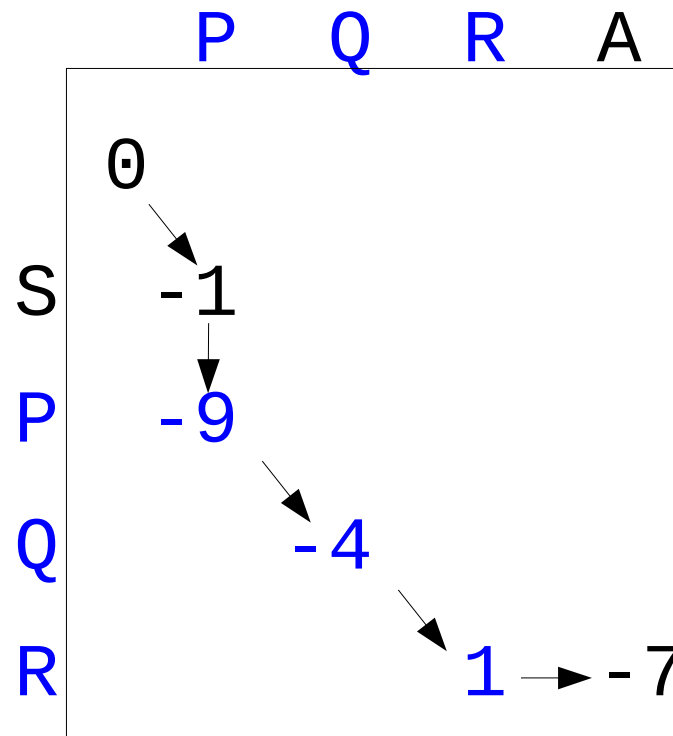
P-QRA
SPQR-

A rigorous method; partial description

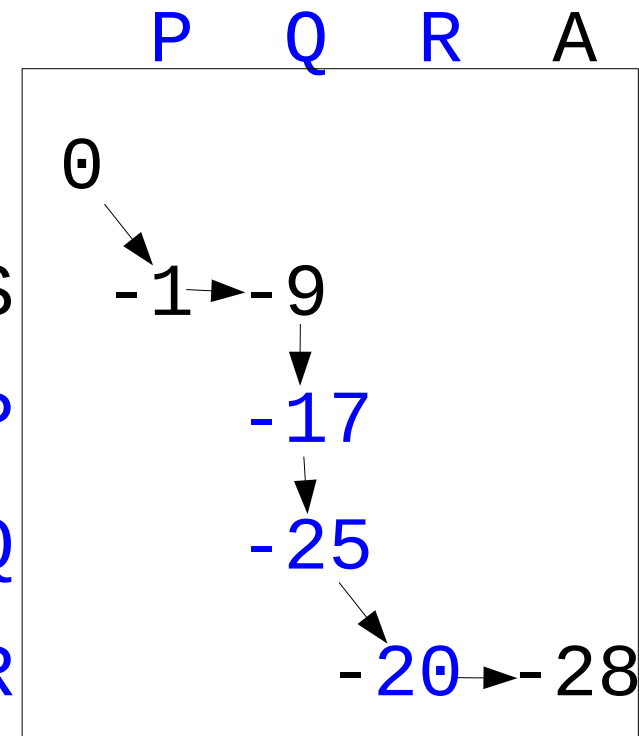
The best alignment competes with many others:



-PQRA
SPQR-



P-QRA
SPQR-



PQ--RA
S-PQR-

How to find the best path through the table?

Suppose we know the scores of 3 particular alignments:

	P	Q	R	A
S	0			
P				
Q			-1	-9
R			9	?

Each blue score corresponds to an incomplete alignment, unknown so far.

From these scores, we deduce the missing score.
How?

How to find the best path through the table?

Suppose we know the scores of 3 particular alignments:

	P	Q	R	A
S	0			
P				
Q			-1	-9
R			9	?

From the blue scores, we deduce the missing score.

3 possibilités:

↘ score $-1 - 1 = -2$

→ score $9 - 8 = 1$

↓ score $-9 - 8 = -17$

How to find the best path through the table?

Suppose we know the scores of 3 particular alignments:

	P	Q	R	A
S	0			
P				
Q			-1	-9
R			9	1

From the blue scores, we deduce the missing score.

3 possibilités:



$$\text{score } -1 - 1 = -2$$



$$\text{score } 9 - 8 = 1$$



$$\text{score } -9 - 8 = -17$$

How to find the best path through the table?

Suppose we know the scores of 3 particular alignments:

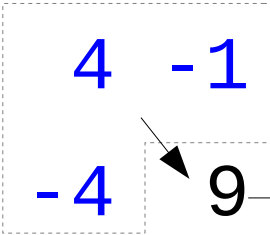
	P	Q	R	A
S	0			
P				
Q		4	-1	-9
R		-4	?	

Now back up and repeat.

How to find the best path through the table?

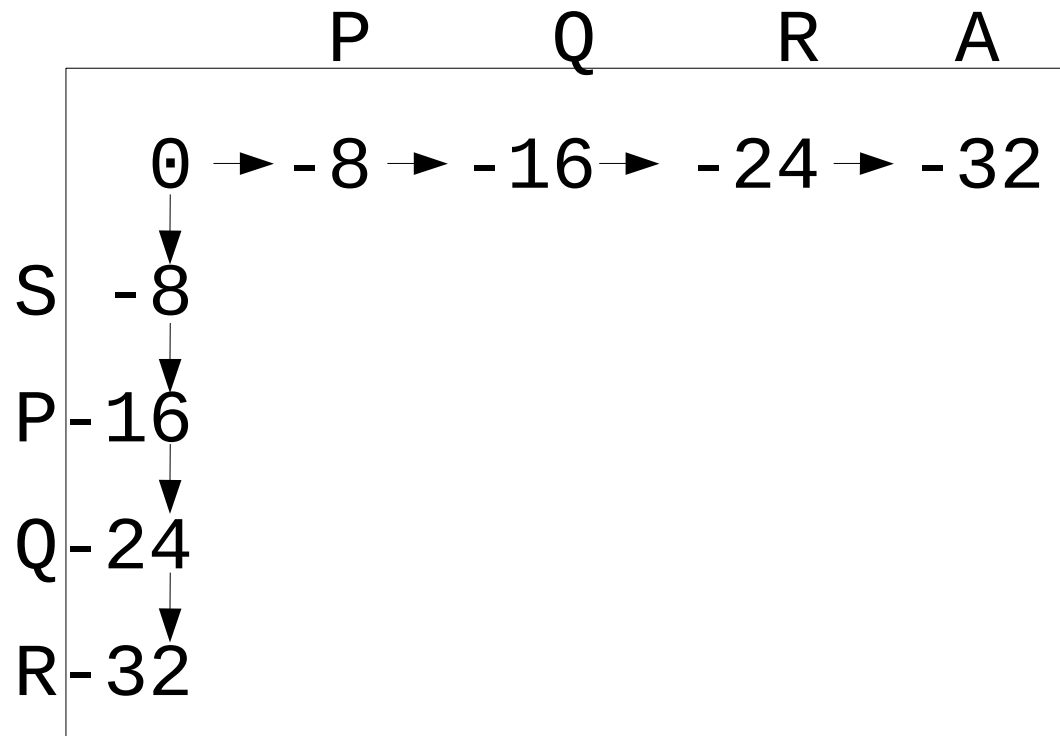
Suppose we know the scores of 3 particular alignments:

	P	Q	R	A
S	0			
P				
Q		4	-1	-9
R		-4	9	1

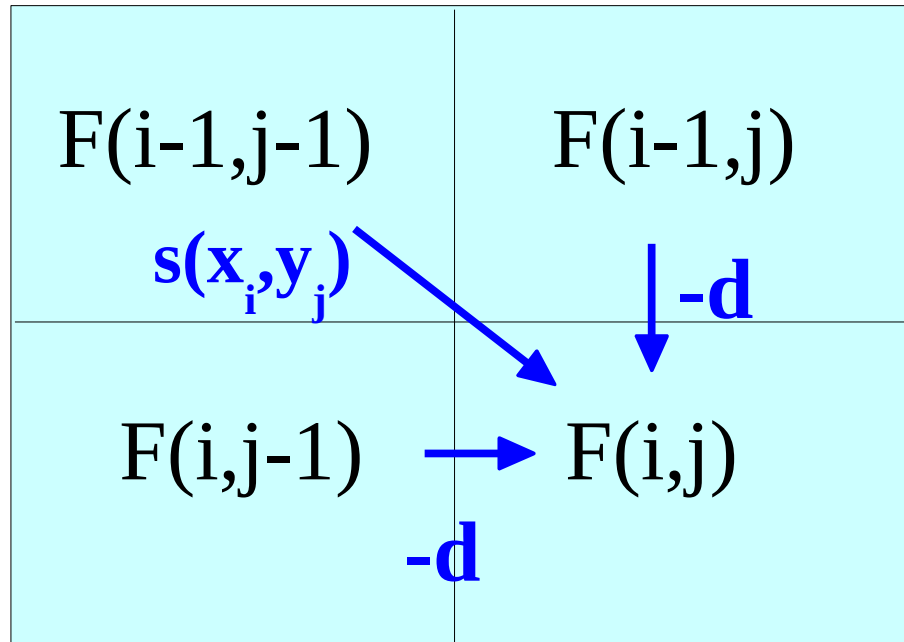
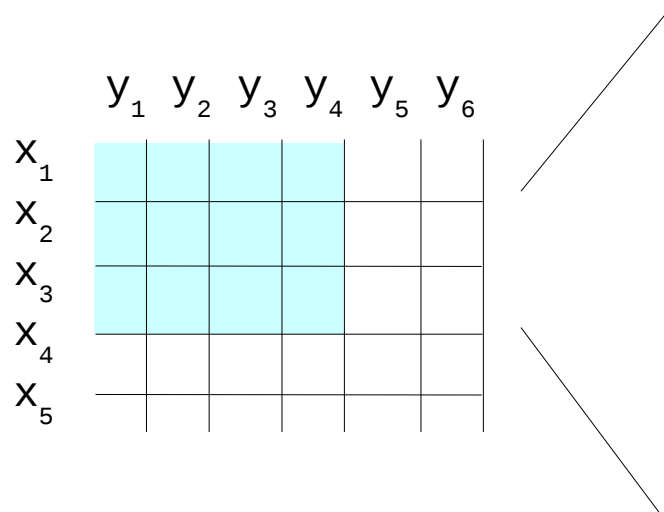


Now back up and repeat.

Needleman-Wunsch method: initialization



Recursive calculation of the score $F(i,j)$



Extending F

Diagram illustrating the calculation of the dot product of two vectors, P and Q .

The vectors are defined as:

$$P = \begin{bmatrix} - \\ S \end{bmatrix}, \quad Q = \begin{bmatrix} - \\ S \end{bmatrix}$$

The dot product calculation is shown in the following table:

	-	P	Q	R	A
-	0	-8	-16	-24	-32
S	-8	-1	-8		
P					
Q					
R					

The diagram shows the calculation of the dot product of P and Q using the formula:

$$P \cdot Q = (-) \cdot (-) + (S) \cdot (S) = 0 + 0 = 0$$

Similarity matrix

	P	Q
S	-1	0

Needleman-Wunsch method

		P	Q	R	A
	0	-8	-16	-24	-32
S	-8	-1	-8	-16	-23
P	-16	-1	-2	-10	-15
Q	-24	-9	4	-1	-9
R	-32	-17	-4	9	1

The diagram illustrates the Needleman-Wunsch method for sequence alignment. It shows a 5x5 matrix of scores for aligning sequences S, P, Q, R with characters P, Q, R, A. The scores are calculated based on a scoring scheme (likely match = 1, mismatch = -1, gap = -2). The optimal alignment path is highlighted by arrows, starting from the top-left (0,0) and ending at the bottom-right (R,A), which has the highest score of 1.

For more details, see Dardel & Képès book

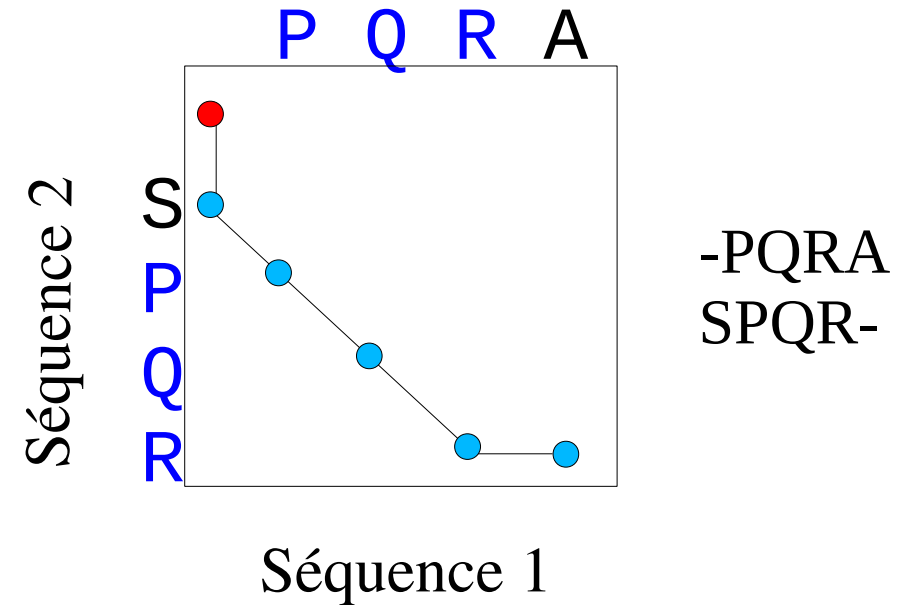
Needleman-Wunsch method

		P	Q	R	A
	0	-8	-16	-24	-32
S	-8	-1	-8	-16	-23
P	-16	-1	-2	-10	-15
Q	-24	-9	4	-1	-9
R	-32	-17	-4	9	1

Needleman-Wunsch method

		P	Q	R	A
S	0	-8	-16	-24	-32
P	-8	-1	-8	-16	-23
Q	-16	-1	-2	-10	-15
R	-24	-9	4	-1	-9
A	-32	-17	-4	9	1

Red arrows indicate the optimal alignment path from (0,0) to (4,4): (0,0) → (0,1) → (1,1) → (1,2) → (2,2) → (2,3) → (3,3) → (4,3) → (4,4).



Multiple alignements: principles

Homologues of the androsterone receptor identified using BLAST

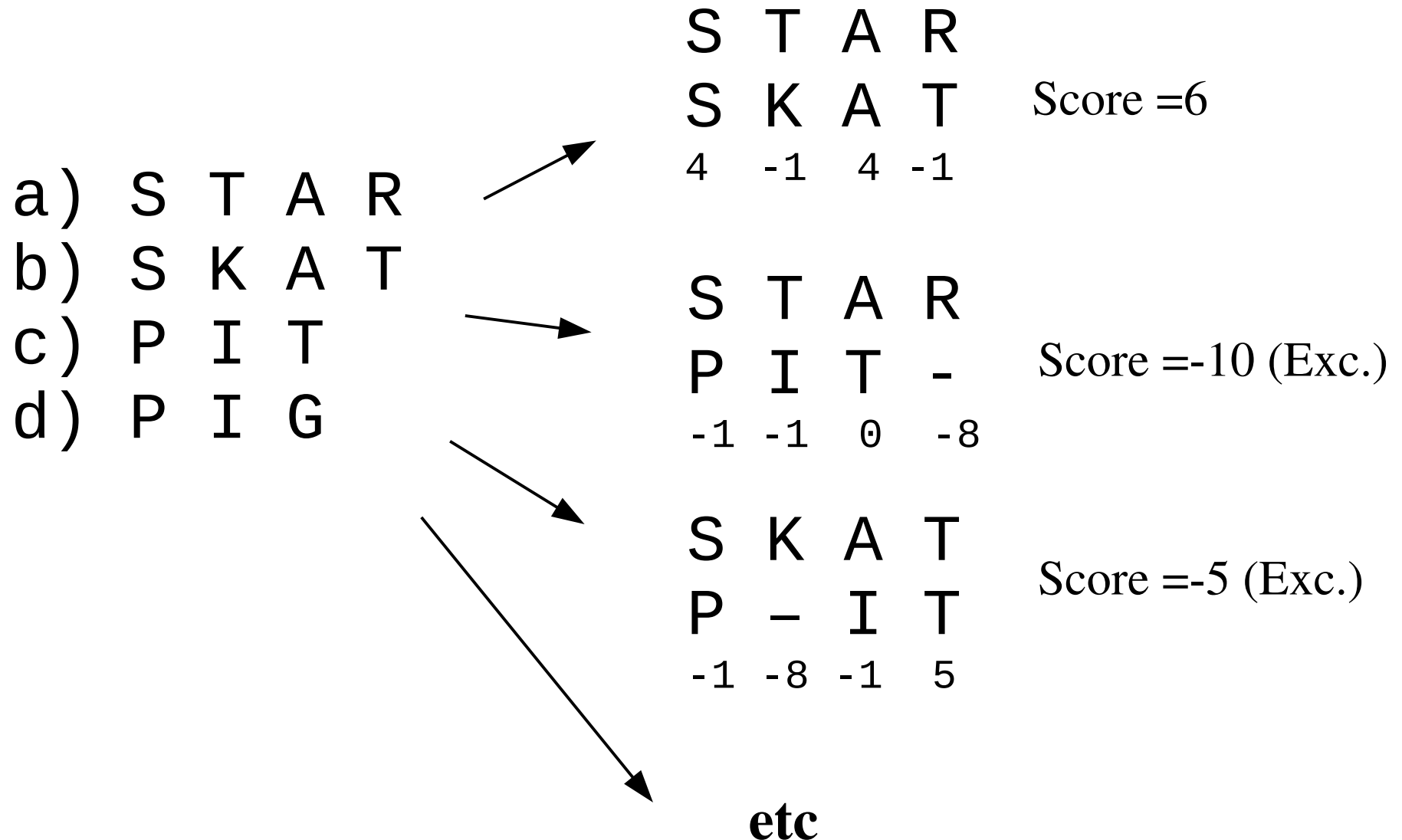
#	ID Swissprot	Hit	Description	Score (bits)	% E Identity *	Match Length	
1	P15207	ANDR_RAT	Androgen receptor.	162	1e-40	100	73
6	P19091	ANDR_MOUSE	Androgen receptor.	162	1e-40	100	73
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42	Q9YH33	ESR1_ORENI	Estrogen receptor (ER-alpha)	98	4e-21	55	72
:	:	:	:	:	:	:	:
:	:	:	:	:	:	:	:
343	Q9N4Q7	NH13_CAEEL	Nuclear hormone receptor nhr-13	54	8e-08	39	66
344	Q23294	NH11_CAEEL	Nuclear hormone receptor nhr-11	54	8e-08	42	66
345	O45460	NH54_CAEEL	Nuclear hormone receptor nhr-54	54	1e-07	37	67
346	Q09565	NH20_CAEEL	Nuclear hormone receptor nhr-20	51	7e-07	34	66
347	Q09587	NH22_CAEEL	Nuclear hormone receptor nhr-22	45	5e-05	32	66
349	P17672	E75B_DROME	Ecdysone-induced protein 75B	40	0.001	37	47
351	P20659	TRX_DROME	Trithorax protein.	31	0.74	26	49
355	P98164	LRP2_HUMAN	Lipoprotein receptor.	30	1.7	27	65

*E = expectation of number of random alignments with a higher score

A heuristic method for multiple sequence alignment in three stages

- 1) Align each pair of sequences
- 2) *Classify* the sequences by similarity: “guide” tree
- 3) Incorporate the sequences progressively into an alignment,
in a sensible order (determined by the tree)

Stage 1: align all sequence pairs

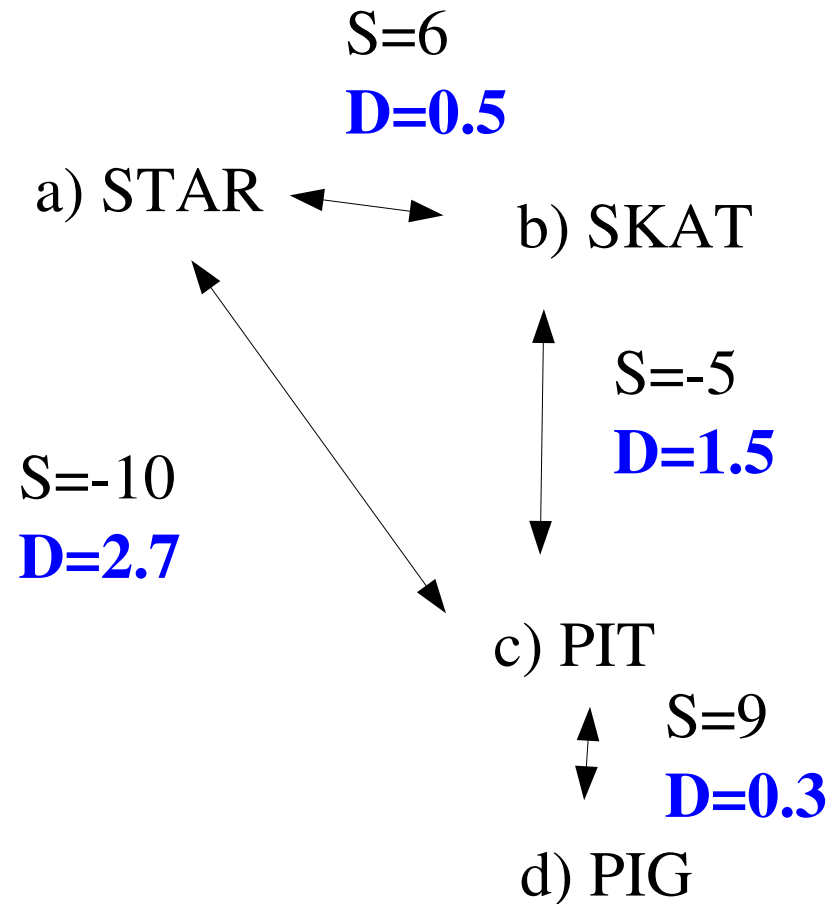


Stage 2: Classify the sequences by similarity: “guide” tree

Stage 3: Incorporate the sequences progressively into the alignment, in a sensible order

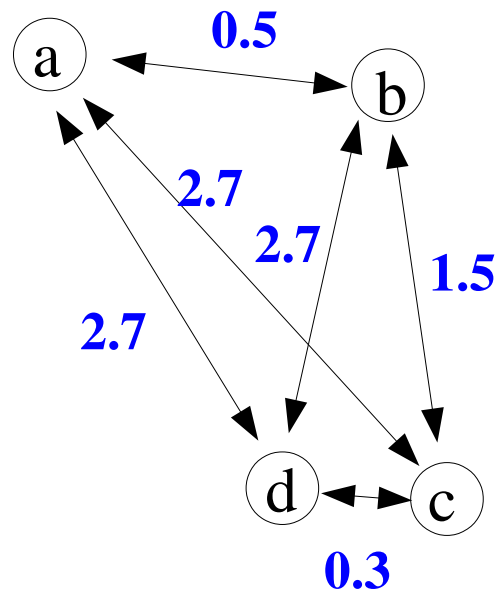
Stage 2: compute “distances” between sequences

Classification methods use distances, rather than similarity

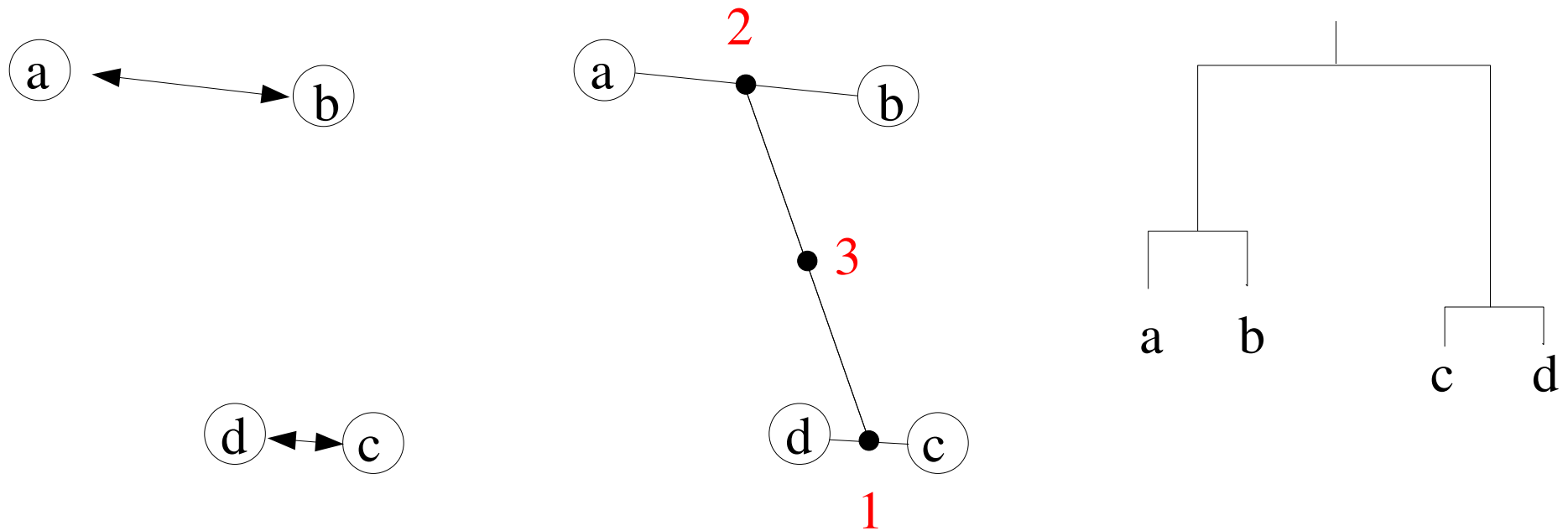


What would be your choice of distance?

Stage 2: compute “distances” between sequences

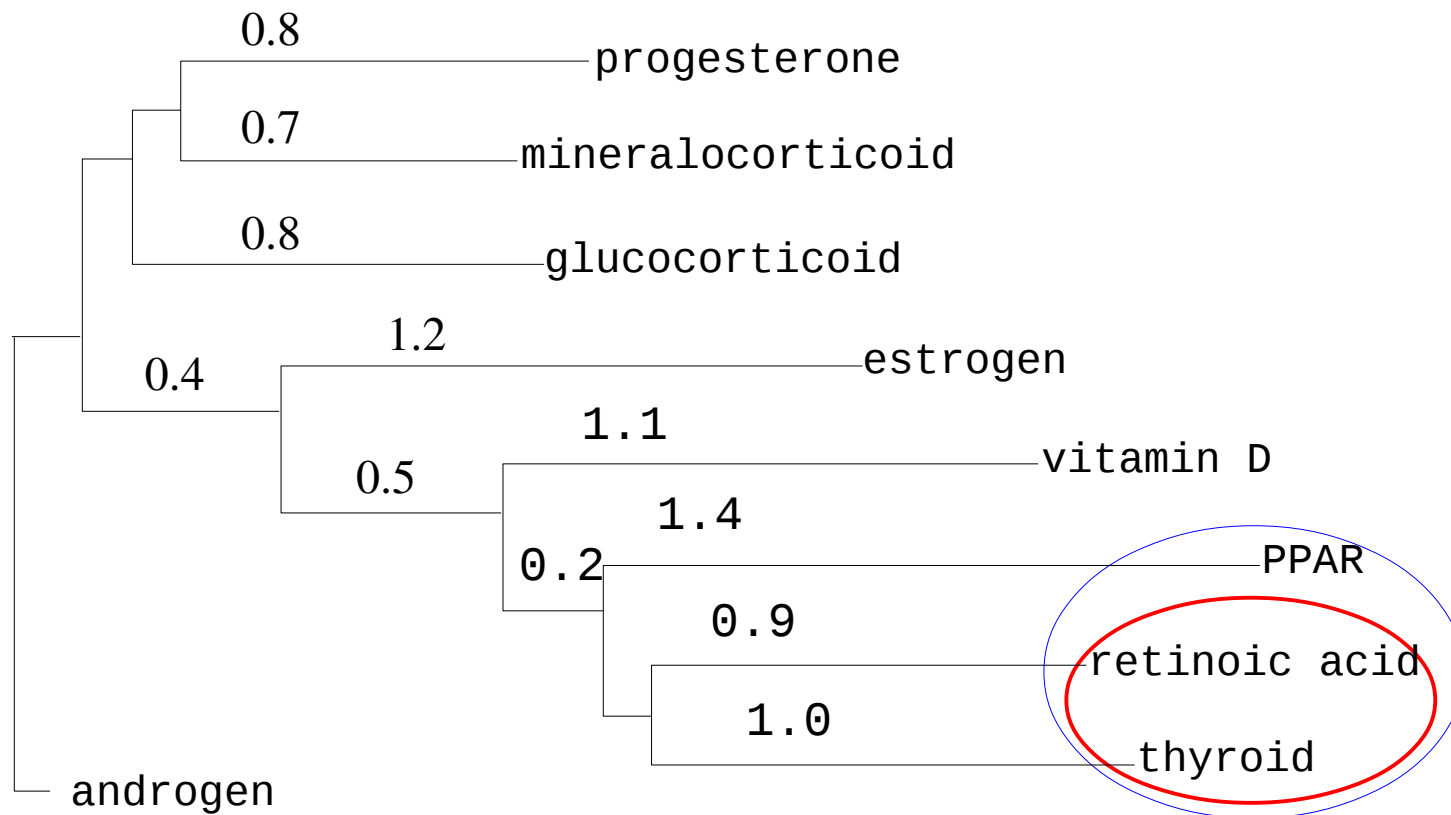


Stage 2: hierarchical classification or “guide” tree



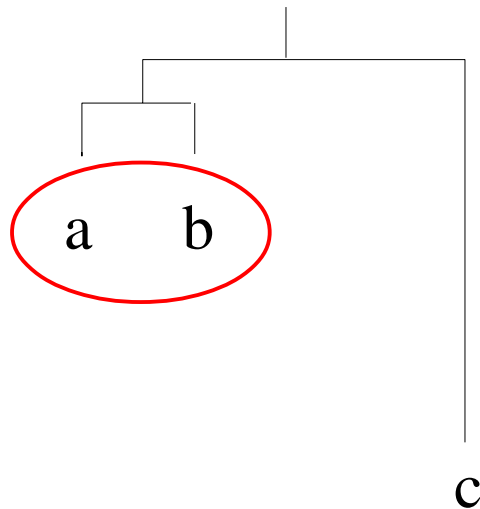
“Unweighted Pair Group Joining with Arithmetic Mean”

Stage 3: sequence alignment, moving up the tree



Stage 3: sequence alignment, moving up the tree

Example with 3 sequences

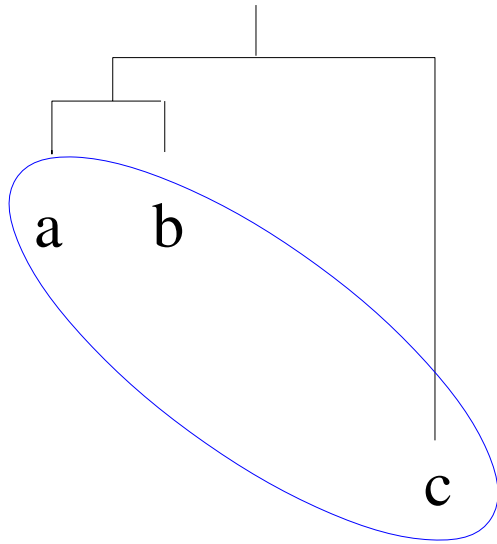


a with b

a) S T A R
b) S K A T

Stage 3: sequence alignment, moving up the tree

Example with 3 sequences



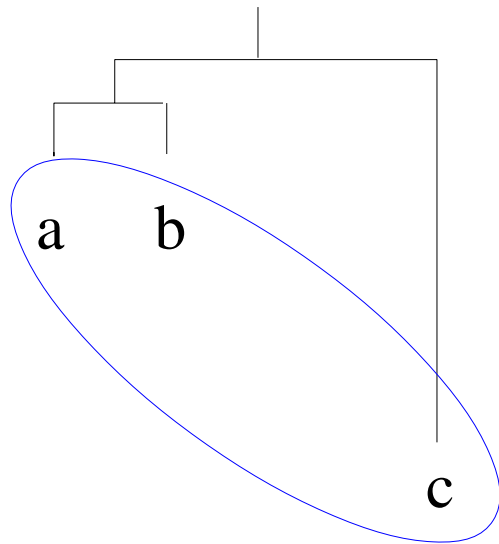
a with b

a) S T A R
b) S K A T

c with {a, b}

Stage 3: sequence alignment, moving up the tree

Example with 3 sequences



a with b

a) S T A R
b) S K A T

c with {a, b}

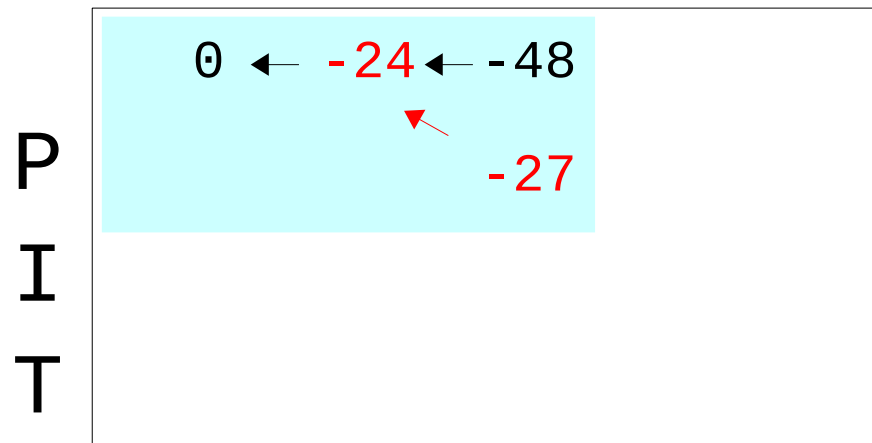
**How to align a sequence with
an alignment?**

“sequence-profile” alignment

We need to generalize slightly our pairwise alignment method....

Sequence-“profile” alignment : dynamic programming, as before

S	T	A	R
S	T	I	R
S	K	A	T



	P
T	-1
T	-1
K	-1
total	-3

gap penalties are tripled

Aligning a sequence with an alignment: computing a “mean” score

An alignment of 3 sequences:

S	T	A	R			P
S	T	I	R		T	-1
S	K	A	T		T	-1
					K	-1
					total	-3

4th sequence y, to be aligned:

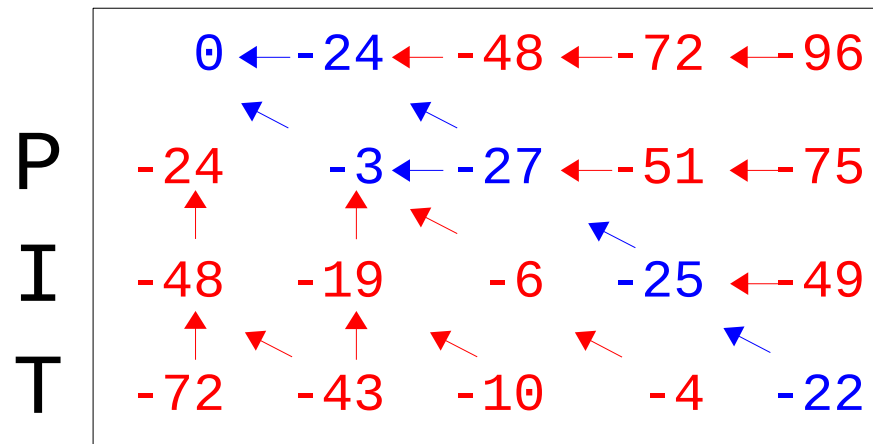
P I T

$$s(a, \begin{bmatrix} b \\ b' \\ b'' \end{bmatrix}) = s(a,b) + s(a,b') + s(a,b'')$$

Sum over pairs

Sequence-“profile” alignment : dynamic programming

S	T	A	R
S	T	I	R
S	K	A	T



S	T	A	R
S	T	I	R
S	K	I	T
P	-	I	T

↘ ↘ ↘ ↘

Aligning two alignments: “profile-profile” alignment

S	T	A	R
S	T	I	R
S	K	A	T

PP
II
GT

$$s\left(\begin{bmatrix} a \\ a' \end{bmatrix}, \begin{bmatrix} b \\ b' \\ b'' \end{bmatrix}\right) = s(a,b) + s(a,b') + s(a,b'') + s(a',b) + s(a',b') + s(a',b'')$$

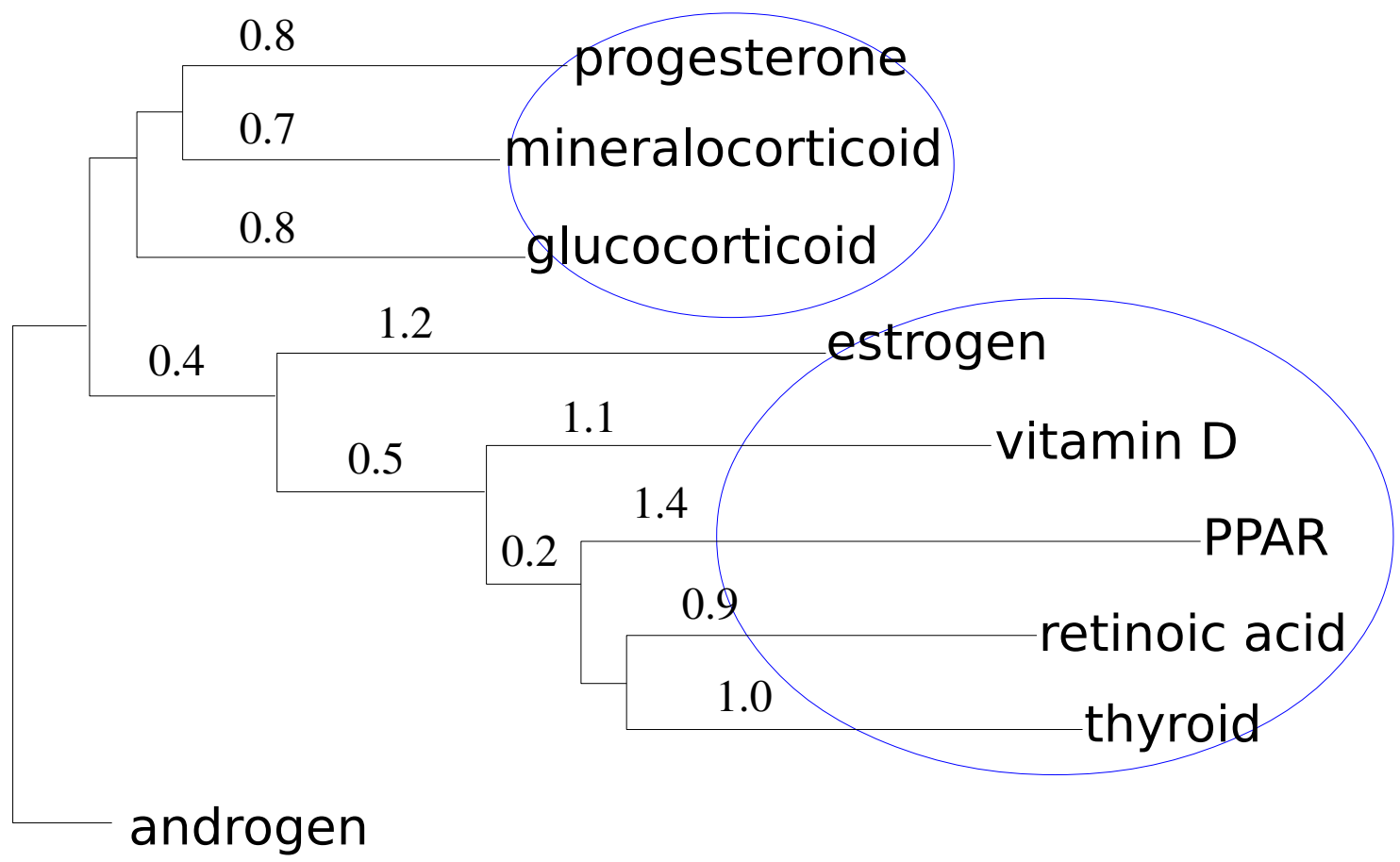


S	T	A	R
S	T	I	R
S	K	A	T
P	-	I	T
P	-	I	G

Sum over pairs

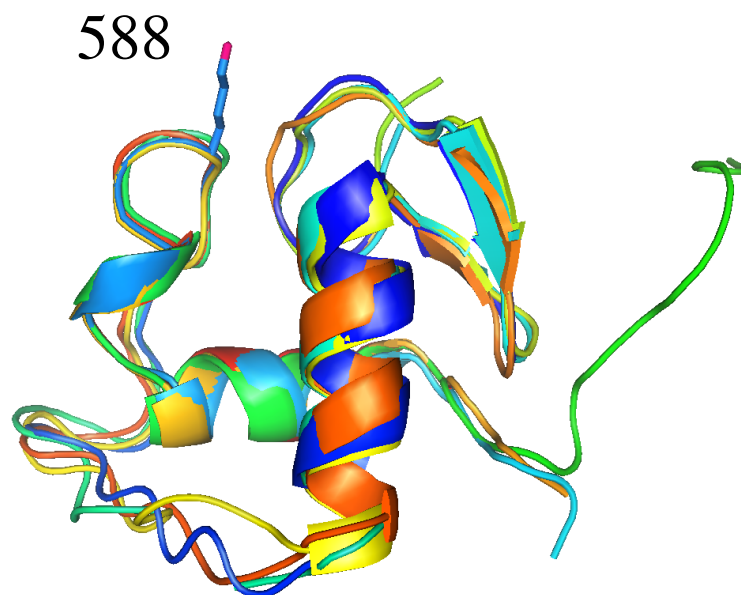
slight generalization of sequence alignment

Stage 3: align the sequences in the order of the guide tree



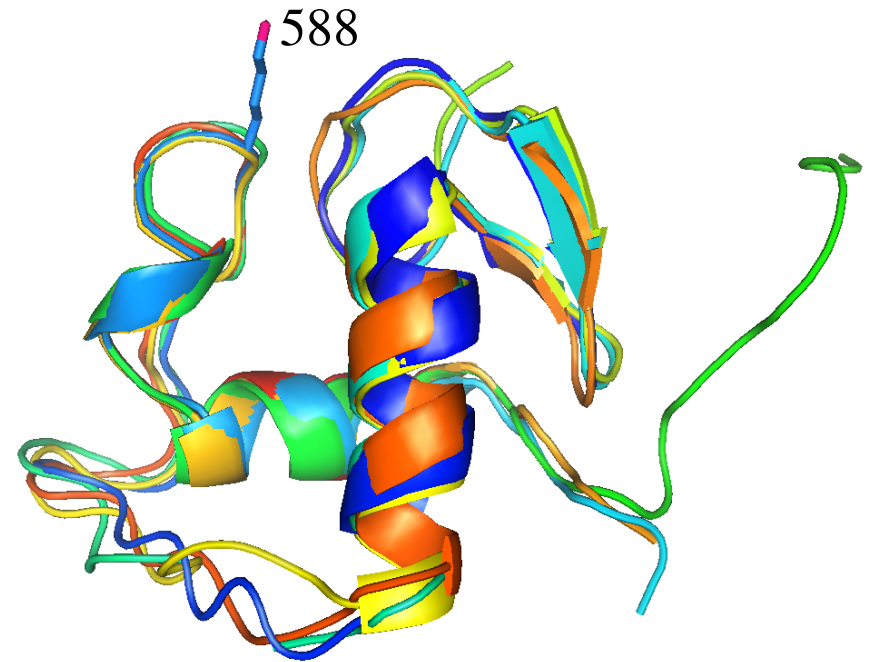
The final result

		584	588	
androgen	VFFKRAAEG--KQKYL	CASRNDCTIDKFRRKNC	CPSCRLRKCY	
progesterone	VFFKRAVEG--HHNYL	CAGRND CIVDKIRRKNC	PACRLRKCY	
Mineralocorticoid	VFFKRAVEG--QHNYL	CAGRND CIIDKIRRKNC	PACRLQKCL	
Glucocorticoid	VFFKRAVEG--QHNYL	CAGRND CIIDKIRRKNC	PACRYRKCL	
Estrogen	AFFKRSIQG--HNDYM	CPATNQCTIDKNRRKSC	QACRLRKCY	
Retinoic acid	GFFRRSIQK--NMVYT	CHRDKNCIINKVTRNRC	QYCRLQKCF	
Vitamin D3	GFFRRSMKR--KALFT	CPFNGDCRITKDNRRHC	QACRLKRCV	
Thyroid	GFFRRTIQKNLHPTYSC	KYDSCCVIDKITRNQC	QLCRFKKCL	
	** : * : . : :	* : * * . *	** : : *	



Experimental testing is needed

- Site-directed mutagenesis of conserved residues
- Detecting an interaction with a substrate or inhibitor
- Determination of the 3D-structure!



Matinées	9h30 – 12h30	Après midis	14h – 17h30
dates	chapitres de la matinée (salles)		après-midi

17/11	Alignements de séquence (SI31)		TP (SI31)
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24/11	Modélisation (SI31)		TP (SI31)
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28/11	Reconnaissance moléculaire 1 + TD		TP (SI35)
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29/11	Modélisation par homologie + TD		TP (SI35)
-------	---------------------------------	--	-----------

3/1	Reconnaissance moléculaire 2 + TD		TP (SI31)
-----	-----------------------------------	--	-----------

5/1	TP		TP (SI31)
-----	----	--	-----------

12/1	TD		TP (SI31)
------	----	--	-----------

19/1 Evaluation: rapport écrit sur un des TPs + contrôle oral

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thomas.gaillard@polytechnique.edu

Laboratoire de Biologie Structurale de la Cellule, Ecole Polytechnique

<http://biology.polytechnique.fr/biocomputing/teach.html>

